

```

> restart;
with(plots):
with(StringTools):
with(LinearAlgebra):
with(DEtools):

#####

Region:='RT'; url:="https://gogov.ru/covid-19/rt#data";

#valp := [9.23983678911537, 4106.99249310287, 0.0561202293832208, 0.0955371316373221,
0.116894940185765, 0.183326912973102, #0.140739820704094, 0.119445148372378, 0.123973323916049,
0.117998388741040, 0.0146398378182489, 0.0882227828533377, #0.0000945735454255790];

valp:=readdata(cat(Region,`3c.txt`));

#####

fdisplay:=proc(f,p)
  print(cat(f,`.jpg`)); #print(cat(f,`.eps`));
  plotsetup(jpeg,plotoutput=cat(f,`.jpg`),plotoptions=`noborder`); print(display(p));
  plotsetup(ps,plotoutput=cat(f,`.eps`),plotoptions=`noborder`); print(display(p));
  plotsetup(default,plotoptions=`noborder`): print(display(p));
end:

pr:=proc(x) print(x); x; end:

grad:=(F,V)->map(q->diff(F,q),V):

linsplit:=(F,V)->subs(map(q->q=0,V),[op(grad(F,V)),F]):

corr:=proc(x,y) local i; seq(x[i]=y[i],i=1..nops(x)): end:

ssum:=(F,V)->convert([seq(F,V)],`+`):

pprod:=(F,V)->convert([seq(F,V)],`*`):

Lag:=proc(t,tx,kx) local i,j;
  ssum(kx[i]*pprod(piecewise(j=i,1,(t-tx[j])/(tx[i]-tx[j])),j=1..nops(tx)),i=1..nops(tx)):
end:

```

```
Lag(t, [ta, tb], [a, b]); Lag(t, [ta, tb, tc], [a, b, c]);
```

```
pi:=evalf(Pi);
```

```
gM:=evalf(solve((1-x)^2=x,x)[2]):
```

```
goldMin:=proc(f,T,epsilon) local a,b,c,d,fa,fb,fc,fd,k;
```

```
  a:=op(1,T); b:=op(2,T); fa:=f(a); fb:=f(b); k:=0;
```

```
  c:=a+(b-a)*gM; fc:=f(c); d:=b-(b-a)*gM; fd:=f(d);
```

```
  while abs(a-b)>epsilon do: k:=k+1;
```

```
    if fc>fd then a:=c; fa:=fc; c:=d; fc:=fd; d:=b-(b-a)*gM; fd:=f(d);
```

```
    else b:=d; fb:=fd; d:=c; fd:=fc; c:=a+(b-a)*gM; fc:=f(c);
```

```
    fi;
```

```
  od: #print(k);
```

```
  (a+b)/2;
```

```
end:
```

```
findMin1:=proc(F,V) local f,df,f0,f1,f2,V0,V1,V2,ff,t,dt,i,j;
```

```
  ff:=V->F(op(evalf(map(exp,V)))); V1:=evalf(map(ln,V)); f1:=F(op(V));
```

```
  f:=[seq(F(seq(evalf(exp(V1[j]+piecewise(j=i,0.0001,0))),j=1..nops(V))),i=1..nops(V))];
```

```
  df:=[seq((f[j]-f1)/0.1,j=1..nops(V))];
```

```
  V0:=V1-0.001*df; f0:=ff(V0); V2:=V1+0.001*df; f2:=ff(V2);
```

```
  dt:=0.0001; while f0<f1 do: V2:=V1; f2:=f1; V1:=V0; f1:=f0; V0:=V0-dt*df; f0:=ff(V0); dt:=dt*1.5; od;
```

```
  dt:=0.0001; while f2<f1 do: V0:=V1; f0:=f1; V1:=V2; f1:=f2; V2:=V2+dt*df; f2:=ff(V2); dt:=dt*1.5; od;
```

```
  t:=goldMin(t->ff(t*V0+(1-t)*V2),0..1,0.001);
```

```
  map(exp,t*V0+(1-t)*V2);
```

```
end:
```

```
findMin:=proc(F,V) local V1,Z1,Z2;
```

```
  Z2:=pr(F(op(V))); V1:=findMin1(F,V); Z1:=pr(chi2(op(V1)));
```

```
  while abs(1-Z1/Z2)>0.0001 do: Z2:=Z1; V1:=findMin1(F,V1); Z1:=pr(chi2(op(V1))); end;
```

```
  V1;
```

```
end:
```

*Region := RT*

*url := "https://gogov.ru/covid-19/rt#data"*

*valp := [9.027883628, 11843.41478, 0.05118252549, 0.08768869384, 0.1219317768, 0.1656771227, 0.1287578269, 0.1090075711,*

0.08241319677, 0.3761057629, 0.01199523996, 0.1086118749, 0.2274905321, 0.0002732039562]

$$\frac{a(t-tb)}{ta-tb} + \frac{b(t-ta)}{tb-ta}$$
$$\frac{a(t-tb)(t-tc)}{(ta-tb)(ta-tc)} + \frac{b(t-ta)(t-tc)}{(tb-ta)(tb-tc)} + \frac{c(t-ta)(t-tb)}{(tc-ta)(tc-tb)}$$
$$\pi := 3.141592654$$

(1

```
> dig:={"0","1","2","3","4","5","6","7","8","9","0"}: val:=proc() global data,i; local j,f; f:=0;
  while not(data[i] in dig) or f=1 and data[i] in {"+"} union dig do:
    if f=1 and not(data[i] in dig) then f:=0; else if data[i]="+" then f:=1; fi fi; i:=i+1: od:
    j:=i; while (data[i] in dig or data[i] in {"-","+"}) do i:=i+1: od: parse(data[j..i-1]);
  end:
  ``; Region; status,data,headers:=HTTP:-Get(url): HTTP:-Code(status); i:=Search("<th>",data):

iter:=proc() global i; local r;
  r:=val(); if data[i]<>"." then NULL else [r,val(),val(),val(),val(),val()],iter() fi;
end:

[iter()]: tA:=[seq(%[nops(%) + 1 - i], i=1..nops(%) )];
dd:=tA[1][1]+piecewise(tA[1][2]=2,-29,tA[1][2]=4,31,0)-1;
T:=map(q->q[4],tA): #writedata(Region || ` -i.txt`,%): #
T3:=map(q->q[5],tA): #writedata(Region || ` -m.txt`,%): #
T1:=map(q->q[6],tA): #writedata(Region || ` -r.txt`,%): #
T2:=map(i->[seq(T[i] - (T1[i] + T3[i]), i=1..nops(T))]: #writedata(Region || ` -h.txt`,%): #
i:='i':
Region; 'T'=T; 'T1'=T1; 'T2'=T2; 'T3'=T3;

nops(T); [i+dd $ i=1..%];
```

``  
RT  
"OK"

```
tA := [[17, 3, 20, 1, 0, 0], [18, 3, 20, 1, 0, 0], [19, 3, 20, 1, 0, 0], [20, 3, 20, 1, 0, 0], [21, 3, 20, 6, 0, 0], [22, 3, 20, 6, 0, 0], [23, 3, 20, 6, 0, 0], [24, 3, 20, 7, 0, 0], [25, 3, 20, 7, 0, 0], [26, 3, 20, 10, 0, 0], [27, 3, 20, 11, 0, 1], [28, 3, 20, 14, 0, 1], [29, 3, 20, 14, 0, 1], [30, 3, 20, 14, 0, 1], [31, 3, 20, 19, 0, 1], [1, 4, 20, 19, 0, 2], [2, 4, 20, 19, 0, 2], [3, 4, 20, 25, 0, 6], [4, 4, 20, 25, 0, 6], [5, 4, 20, 25, 0, 6], [6, 4, 20, 41, 0, 6], [7, 4, 20, 41, 0, 8], [8, 4, 20, 41, 0, 10], [9, 4, 20, 50, 0, 10], [10, 4, 20, 50, 0, 11], [11, 4, 20, 73, 0, 11], [12, 4, 20, 73, 0, 14],
```



[17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115]

(2)

```
> =====` ;
`VERHULST FITAING` ;
`=====` ;
```

```
=====
VERHULST FITAING
=====
```

(3)

```
> h:=x->x;
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]
],i=1..nops(%%))]:
display(
plot([%%,%,%],style=point),
plot([%%,%,%],legend=[``,``,``]),
title=` N[i]`,titlefont=[roman,15],gridlines=true
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%
[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]
],i=1..nops(%%))]:
display(
plot([%%,%,%],style=point),
plot([%%,%,%],legend=[``,``,``]),
title=` N[i]`,titlefont=[roman,15],gridlines=true
);
```

$h := x \mapsto x$

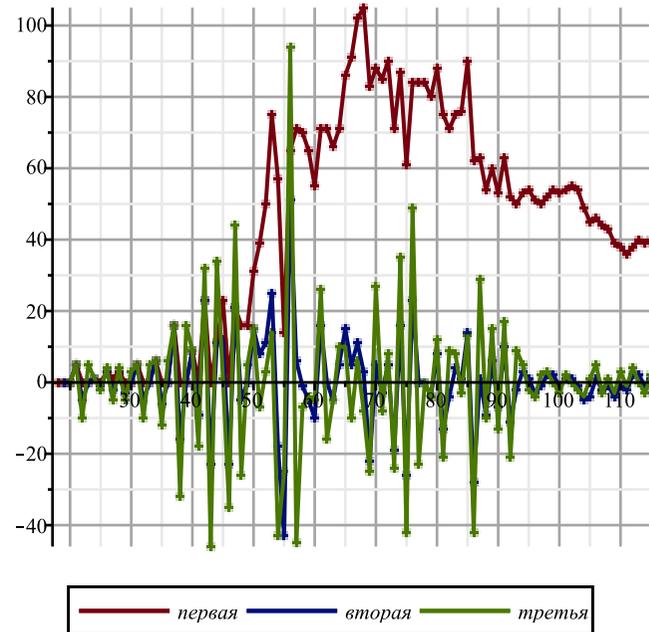
[0, 0, 0, 5, 0, 0, 1, 0, 3, 1, 3, 0, 0, 5, 0, 0, 6, 0, 0, 16, 0, 0, 9, 0, 23, 0, 11, 23, 0, 21, 16, 16, 31, 39, 50, 75, 57, 14, 65, 71, 70, 65, 55, 71, 71, 66, 71, 86, 91, 102, 105, 83, 88, 85, 90, 71, 87, 61, 84, 84, 84, 80, 88, 75, 71, 75, 76, 90, 62, 63, 54, 60, 53, 63, 52, 50, 53, 54, 51, 50, 52, 54,

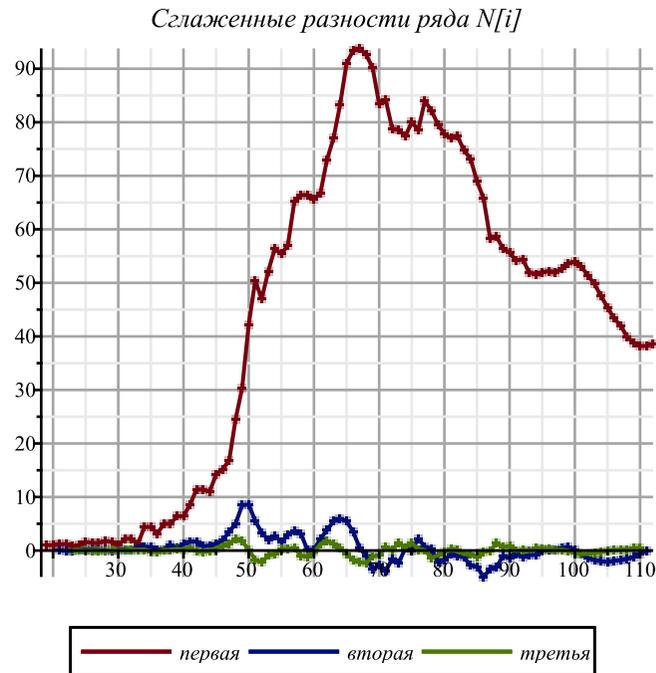
53, 54, 55, 54, 49, 45, 46, 44, 43, 39, 38, 36, 38, 40, 39, 40]

[0, 0, 5, -5, 0, 1, -1, 3, -2, 2, -3, 0, 5, -5, 0, 6, -6, 0, 16, -16, 0, 9, -9, 23, -23, 11, 12, -23, 21, -5, 0, 15, 8, 11, 25, -18, -43, 51, 6, -1, -5, -10, 16, 0, -5, 5, 15, 5, 11, 3, -22, 5, -3, 5, -19, 16, -26, 23, 0, 0, -4, 8, -13, -4, 4, 1, 14, -28, 1, -9, 6, -7, 10, -11, -2, 3, 1, -3, -1, 2, 2, -1, 1, 1, -1, -5, -4, 1, -2, -1, -4, -1, -2, 2, 2, -1, 1]

[0, 5, -10, 5, 1, -2, 4, -5, 4, -5, 3, 5, -10, 5, 6, -12, 6, 16, -32, 16, 9, -18, 32, -46, 34, 1, -35, 44, -26, 5, 15, -7, 3, 14, -43, -25, 94, -45, -7, -4, -5, 26, -16, -5, 10, 10, -10, 6, -8, -25, 27, -8, 8, -24, 35, -42, 49, -23, 0, -4, 12, -21, 9, 8, -3, 13, -42, 29, -10, 15, -13, 17, -21, 9, 5, -2, -4, 2, 3, 0, -3, 2, 0, -2, -4, 1, 5, -3, 1, -3, 3, -1, 4, 0, -3, 2]

Разности ряда  $N[i]$





```
> h:=x->evalf(ln(x));
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=[``,``,``]),
  title=`ln(N[i])`,titlefont=[roman,15],gridlines=true
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%
[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=[``,``,``]),
```

```
title = `ln(N[i])`,titlefont=[roman,15],gridlines=true);
```

$h := x \mapsto \text{evalf}(\ln(x))$

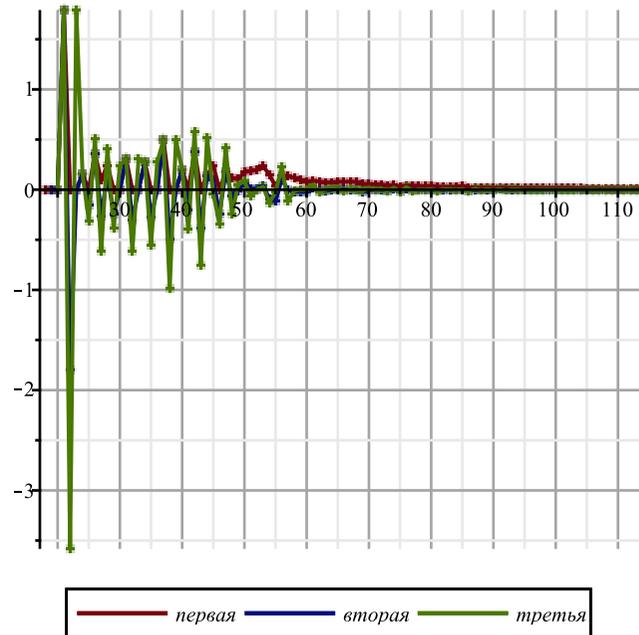
```
[0., 0., 0., 1.791759469, 0., 0., 0.154150680, 0., 0.356674944, 0.095310180, 0.241162057, 0., 0., 0.305381649, 0., 0., 0.274436845, 0., 0., 0.494696243, 0., 0., 0.198450938, 0., 0.378436436, 0., 0.140357358, 0.242012035, 0., 0.179201430, 0.117783036, 0.105360515, 0.177099613, 0.185805881, 0.196710294, 0.237328186, 0.148905560, 0.033415997, 0.142004782, 0.135057722, 0.117387544, 0.097896017, 0.075950913, 0.090219877, 0.082749574, 0.071227509, 0.071351200, 0.080117315, 0.078319579, 0.081061038, 0.077102394, 0.057001354, 0.057084238, 0.052207127, 0.052459579, 0.039526437, 0.046395951, 0.031292628, 0.041549003, 0.039891329, 0.038360868, 0.035214906, 0.037355786, 0.030771659, 0.028283104, 0.029032424, 0.028584120, 0.032825704, 0.022002307, 0.021872075, 0.018374114, 0.020027371, 0.017363254, 0.020254671, 0.016414510, 0.015533086, 0.016205828, 0.016245845, 0.015104685, 0.014590279, 0.014951400, 0.015293416, 0.014786153, 0.014843593, 0.014895333, 0.014411779, 0.012900008, 0.011702123, 0.011822291, 0.011178978, 0.010805483, 0.009700362, 0.009361980, 0.008789119, 0.009194355, 0.009587801, 0.009260425, 0.009409620]
```

```
[0., 0., 1.791759469, -1.791759469, 0., 0.154150680, -0.154150680, 0.356674944, -0.261364764, 0.145851877, -0.241162057, 0., 0.305381649, -0.305381649, 0., 0.274436845, -0.274436845, 0., 0.494696243, -0.494696243, 0., 0.198450938, -0.198450938, 0.378436436, -0.378436436, 0.140357358, 0.101654677, -0.242012035, 0.179201430, -0.061418394, -0.012422521, 0.071739098, 0.008706268, 0.010904413, 0.040617892, -0.088422626, -0.115489563, 0.108588785, -0.006947060, -0.017670178, -0.019491527, -0.021945104, 0.014268964, -0.007470303, -0.011522065, 0.000123691, 0.008766115, -0.001797736, 0.002741459, -0.003958644, -0.020101040, 0.000082884, -0.004877111, 0.000252452, -0.012933142, 0.006869514, -0.015103323, 0.010256375, -0.001657674, -0.001530461, -0.003145962, 0.002140880, -0.006584127, -0.002488555, 0.000749320, -0.000448304, 0.004241584, -0.010823397, -0.000130232, -0.003497961, 0.001653257, -0.002664117, 0.002891417, -0.003840161, -0.000881424, 0.000672742, 0.000040017, -0.001141160, -0.000514406, 0.000361121, 0.000342016, -0.000507263, 0.000057440, 0.000051740, -0.000483554, -0.001511771, -0.001197885, 0.000120168, -0.000643313, -0.000373495, -0.001105121, -0.000338382, -0.000572861, 0.000405236, 0.000393446, -0.000327376, 0.000149195]
```

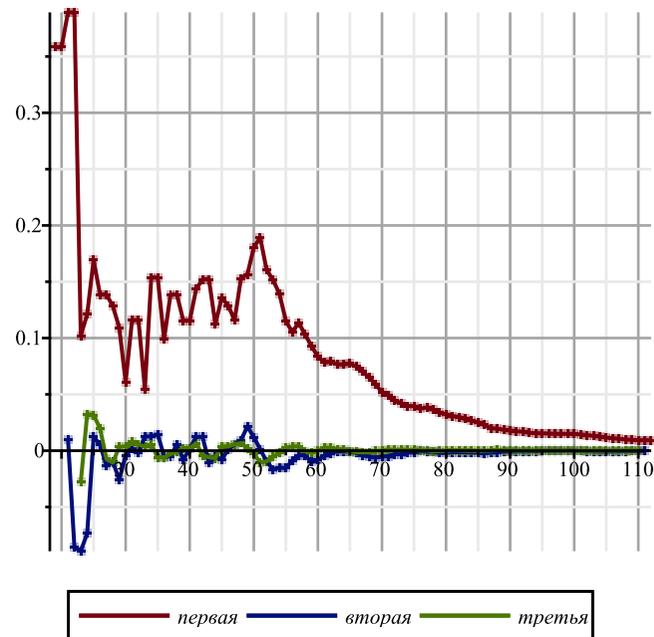
```
[0., 1.791759469, -3.583518938, 1.791759469, 0.154150680, -0.308301360, 0.510825624, -0.618039708, 0.407216641, -0.387013934, 0.241162057, 0.305381649, -0.610763298, 0.305381649, 0.274436845, -0.548873690, 0.274436845, 0.494696243, -0.989392486, 0.494696243, 0.198450938, -0.396901876, 0.576887374, -0.756872872, 0.518793794, -0.038702681, -0.343666712, 0.421213465, -0.240619824, 0.048995873, 0.084161619, -0.063032830, 0.002198145, 0.029713479, -0.129040518, -0.027066937, 0.224078348, -0.115535845, -0.010723118, -0.001821349, -0.002453577, 0.036214068, -0.021739267, -0.004051762, 0.011645756,
```

0.008642424, -0.010563851, 0.004539195, -0.006700103, -0.016142396, 0.020183924, -0.004959995, 0.005129563,  
-0.013185594, 0.019802656, -0.021972837, 0.025359698, -0.011914049, 0.000127213, -0.001615501, 0.005286842,  
-0.008725007, 0.004095572, 0.003237875, -0.001197624, 0.004689888, -0.015064981, 0.010693165, -0.003367729, 0.005151218,  
-0.004317374, 0.005555534, -0.006731578, 0.002958737, 0.001554166, -0.000632725, -0.001181177, 0.000626754, 0.000875527,  
-0.000019105, -0.000849279, 0.000564703,  $-5.700 \cdot 10^{-6}$ , -0.000535294, -0.001028217, 0.000313886, 0.001318053,  
-0.000763481, 0.000269818, -0.000731626, 0.000766739, -0.000234479, 0.000978097, -0.000011790, -0.000720822, 0.000476571 ]

Разности ряда  $\ln(N[i])$



Сглаженные разности ряда  $\ln(N[i])$



```

> f_:=d->sum(a[j]*d^j,j=0..n); fe_:=d->sum(a[j]*d^j,j=0..ne);

M:='M':
ff:=x->M*(1-1/(exp(x)+1)); ff_:=unapply(solve(y=ff(x),x),y); diff(ff_(x),x); dff_:=unapply
(simplify(% ,x),x);
ffe:=x->exp(x); ffe_:=unapply(solve(y=ffe(x),x),y); diff(ff_(x),x); dffe_:=unapply(simplify(% ,
x),x);

sigma:=x->simplify(sqrt(x));

chi2:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dff_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));
chi2e:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dffe_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));

F:=proc(T,chi2,f_) chi2(T,f_);
  indets(%); grad(% ,%); subs(solve(% ,%),f_(i)); unapply(% ,i);
end:

```

$$f_- := d \mapsto \sum_{j=0}^n a_j \cdot d^j$$

$$fe_- := d \mapsto \sum_{j=0}^{ne} a_j \cdot d^j$$

$$ff := x \mapsto M \cdot \left( 1 - \frac{1}{e^x + 1} \right)$$

$$ff_- := y \mapsto \ln\left(\frac{y}{M-y}\right)$$

$$\frac{\left( \frac{1}{M-x} + \frac{x}{(M-x)^2} \right) (M-x)}{x}$$

$$dff_- := x \mapsto \frac{M}{(M-x) \cdot x}$$

$$ffe := x \mapsto e^x$$

$$ffe_- := y \mapsto \ln(y)$$

$$\frac{1}{x}$$

$$dffe_- := x \mapsto \frac{1}{x}$$

$$\sigma := x \mapsto \text{simplify}(\sqrt{x})$$

$$\chi^2 := (T, f_-) \rightarrow \text{simplify} \left( \sum_{k=1}^{nops(T)} \frac{\text{evalf}(ff_-(T_k) - f_-(k))^2}{dff_-(T_k)^2 \sigma(T_k)^2} \right)$$

$$\chi^2e := (T, f_-) \rightarrow \text{simplify} \left( \sum_{k=1}^{nops(T)} \frac{\text{evalf}(ffe_-(T_k) - f_-(k))^2}{dffe_-(T_k)^2 \sigma(T_k)^2} \right)$$

```
> n:=1: ne:=n: 'f(t) '=Sum(a[j]*t^j,j=0..n);
```

```

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],
gridlines=true);

d1:=fsolve(f(d)=0.5*M,d=30)+dd; K_:=M; alpha_:=coeff(nu(t),t,1);

n:=4: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);

[seq([i,(
(T[i-dd]-T[i-dd-1])/(T2[i-dd]+T2[i-dd-1])/((1-T[i-dd]/M)+(1-T[i-dd-1]/M))
)*4],i=1+dd+1..nops(T)+dd): [seq(#[i][1],([i-1][2]+[i][2]+#[i+1][2])/3],i=2..nops(%)-1)]:
Palpha:=display(plot(#[%],color=blue),plot(#[%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],

```

```
gridlines=true) :  
display(Palpha,%) ;
```

$$f(t) = \sum_{j=0}^1 a_j t^j$$

*Approximation of the infection schedule by the solution of the Verhulst equation*

$$M := 4273.369418$$

$$N(t) = 4273.369418 - \frac{4273.369418}{e^{0.09650977365 t - 5.949179454} + 1}$$

$$Chi2 := 1428.078908$$

*Next day forecast: 4170*

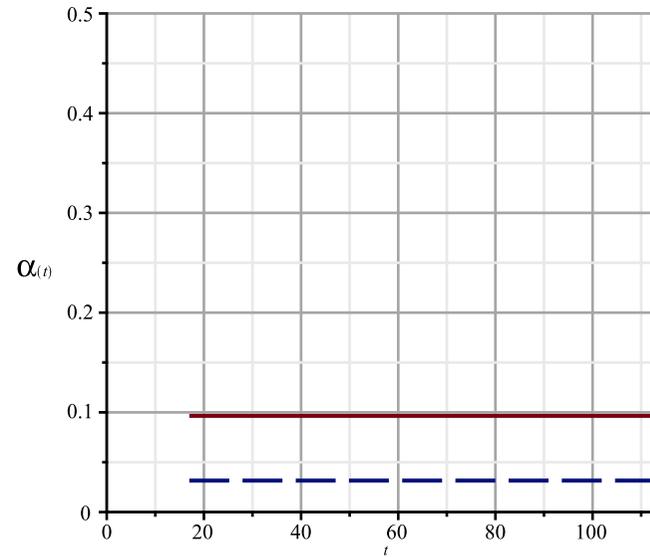
*The level of 0.5 M is reached at 48 apr*

*The level of 0.85 M is reached at 66 apr*

*Approximation of the infection schedule by solving the Malthus equation*

$$N(t) = e^{0.03156622675 t + 5.516743793} [0.09650977365]$$

*Коэффициент заражения*



Ферхюльст Мальтус

$$dI := 77.64328471$$

$$K_ := 4273.369418$$

$$alpha_ := 0.09650977365$$

$$f(t) = \sum_{j=0}^4 a_j t^j$$

*Approximation of the infection schedule by the solution of the Verhulst equation*

$$M := 4273.369418$$

$$N(t) = 4273.369418 - \frac{4273.369418}{e^{5.318491734 \cdot 10^{-7} t^4 - 0.0001022337263 t^3 + 0.005873980102 t^2 + 0.01569822774 t - 6.928438323} + 1}$$

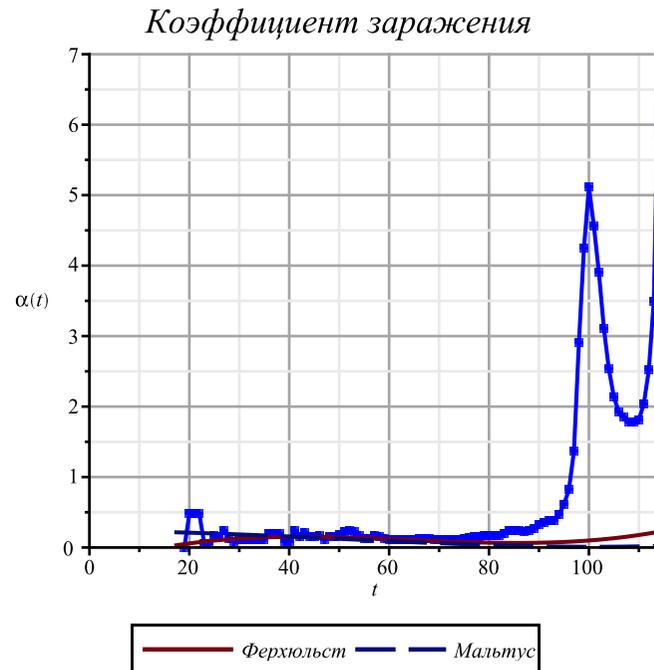
$$Chi2 := 63.98818627$$

Next day forecast: 4218

The level of 0.5 M is reached at 46 apr  
 The level of 0.85 M is reached at 70 apr

Approximation of the infection schedule by solving the Malthus equation

$$N(t) = e^{1.079419773 \cdot 10^{-7} t^4 - 0.00001490350189 t^3 - 0.0008816760899 t^2 + 0.2179282127 t - 0.4422165450} \cdot [-0.259498454300000, 0.0231962385800000, -0.000408816220200000, 2.127396694 \cdot 10^{-6}]$$



```
> df:=unapply(diff(f(i),i),i): ddf:=unapply(diff(f(i),i,i),i):
```

```
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(90,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(90,dd+nops(T))),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i))],[i+dd,T[i]-3*sqrt(T[i))]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..80,1..M*1.1],labels=[t,N(t)],gridlines=true
```

```

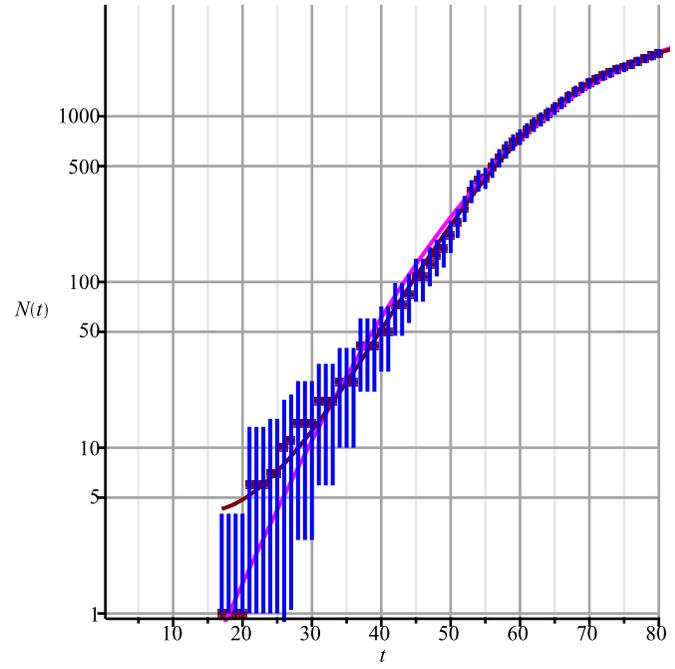
);

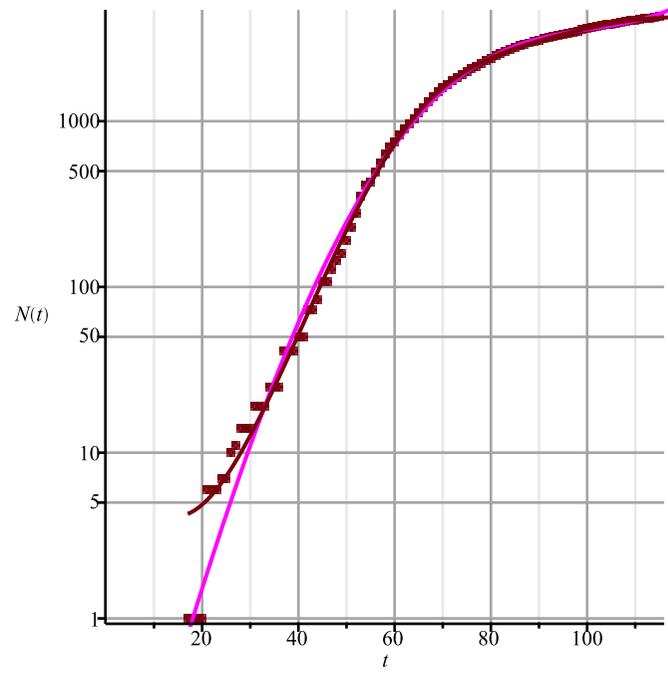
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(120,dd+nops(T))),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

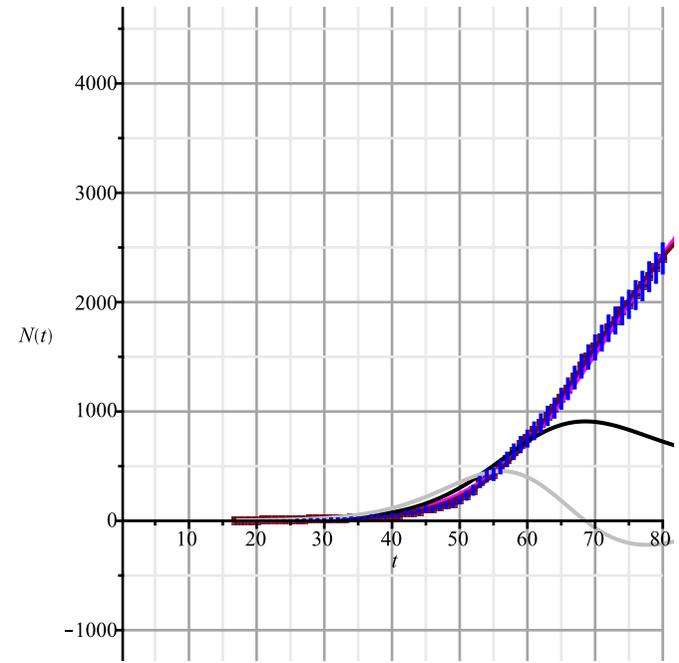
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),90)),
  plot(10*df(i-dd),i=1+dd..max(dd+nops(T),120),color=black),
  plot(100*ddf(i-dd),i=1+dd..max(dd+nops(T),120),color=gray),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..80,-M*0.3..M*1.1],labels=[t,N(t)],gridlines=true
);

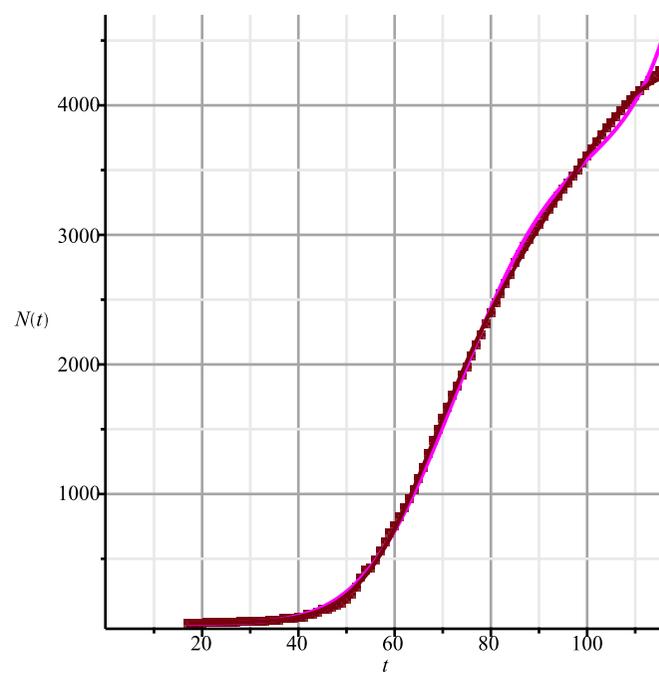
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),120)),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

```

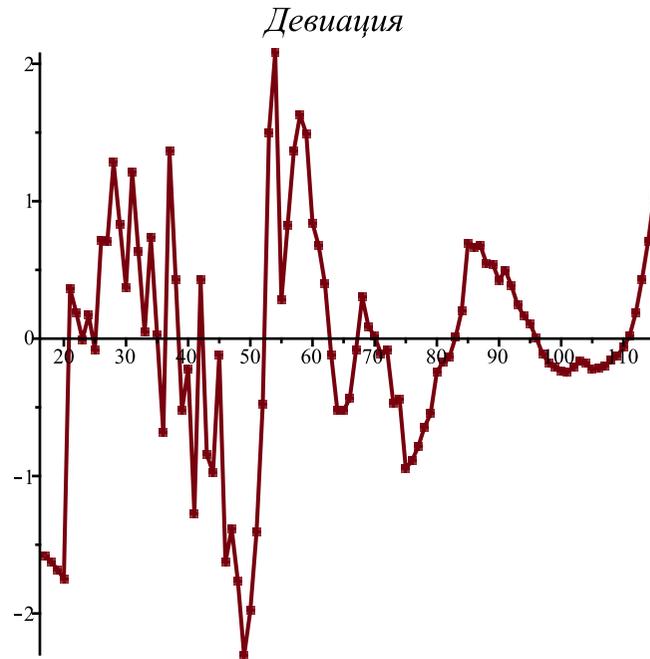








```
> dT:=[i, (T[i-dd]-f(i-dd))/sigma(f(i-dd))] $ i=1+dd..dd+nops(T):
display( plot(%), plot(% ,style=point,symbolsize=8,symbol=solidcircle),title = ` ` ,titlefont=
[roman,20] );
```



```

> ===== ` ;
  `FORECAST` ;
  ===== ` ;

=====
                                FORECAST
=====

> proc3:=proc (E)
  E[1]*convert (map (X->X^coeff (E[2] ,X,1) ,M) , `*` ) ;
end:

proc2:=proc (X,E)
  proc3 (E) * (coeff (E[3] ,X,1) -coeff (E[2] ,X,1)) ;
end:

proc1:=proc (X)
  convert (map (E->proc2 (X,E) ,L) , `+` ) ;
end:

```

```
> A:='A': B:='B': C:='C': Q:='Q': M:=[A,B,C,Q];
```

```
L:=
  [(A+C)*P[`01`],0,A],
  [(B/K)*P[`12`],A,B],
  [P[`23`],B,C],
  [P[`10`],A,0], [P[`20`],B,Q], [P[`30`],C,0]
]: Matrix(%);
```

```
eqs:=map(X->Diff(X,t)=procl(X),M); Vector(%);
```

$M := [A, B, C, Q]$

$$\begin{bmatrix} (A+C)P_{01} & 0 & A \\ \frac{BP_{12}}{K} & A & B \\ P_{23} & B & C \\ P_{10} & A & 0 \\ P_{20} & B & Q \\ P_{30} & C & 0 \end{bmatrix}$$

$$eqs := \left[ \frac{\partial}{\partial t} A = (A+C)P_{01} - \frac{BP_{12}A}{K} - P_{10}A, \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B, \frac{\partial}{\partial t} C = P_{23}B - P_{30}C, \frac{\partial}{\partial t} Q = P_{20}B \right]$$

$$\begin{cases} \frac{\partial}{\partial t} A = (A + C) P_{01} - \frac{B P_{12} A}{K} - P_{10} A \\ \frac{\partial}{\partial t} B = \frac{B P_{12} A}{K} - P_{23} B - P_{20} B \\ \frac{\partial}{\partial t} C = P_{23} B - P_{30} C \\ \frac{\partial}{\partial t} Q = P_{20} B \end{cases}$$

(6)

```
> v:=M; alpha:='alpha': K:=k0; tA:=[-7,15,35,50,58,62,78,nops(T)+dd]; kA:=['k1x||i' $ i=1..nops(tA)
];
par:=[d0,k0,op(kA),k2a,k2b,k2c,k3]; kappa:=0; 0.011/365;
param:=[
  P[`01`] = kappa, P[`12`] = alpha(t,op(kA)), P[`23`] = beta(t,k2a,k2b,k2c),
  P[`10`] = kappa, P[`20`] = k3, P[`30`] = kappa
];
init:=[ A(-d0)=K, B(-d0)=1, C(-d0)=0, Q(-d0)=0 ];
```

$$v := [A, B, C, Q]$$

$$K := k0$$

$$tA := [-7, 15, 35, 50, 58, 62, 78, 115]$$

$$kA := [k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8]$$

$$par := [d0, k0, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8, k2a, k2b, k2c, k3]$$

$$\kappa := 0$$

$$0.00003013698630$$

$$param := [P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b, k2c), P_{10} = 0, P_{20} = k3, P_{30} = 0]$$

$$init := [A(-d0) = k0, B(-d0) = 1, C(-d0) = 0, Q(-d0) = 0]$$

(7)

```
> Eqs:=subs(map(q->q(t),v),Diff=diff,param,eqs); #dsolve(%);
```

$$Eqs := \left[ \frac{d}{dt} A(t) = - \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0}, \frac{d}{dt} B(t) \right. \\ = \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0} - \beta(t, k2a, k2b, k2c) B(t) - k3 B(t), \frac{d}{dt} C(t) = \beta(t, k2a, k2b, \\ \left. k2c) B(t), \frac{d}{dt} Q(t) = k3 B(t) \right]$$

```
> N:='N': A:='A': B:='B': C:='C': Q:='Q': val:=valp:
```

```
#alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[2],Lag(t,tA[1..3],kA[1..3]),
# seq(op([t<tA[i+1],(Lag(t,tA[i-1..i+1],kA[i-1..i+1])+Lag(t,tA[i..i+2],kA[i..i+2]))/2]),i=2..nops
(kA)-2),
#t<tA[nops(tA)],Lag(t,tA[nops(tA)-2..nops(tA)],kA[nops(kA)-2..nops(kA)]),
#kA[nops(kA)])),t,op(kA)):
```

```
alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[3],Lag(t,tA[1..4],kA[1..4]),
seq(op([t<tA[i+1],Lag(t,tA[i-1..i+2],kA[i-1..i+2])]),i=3..nops(kA)-2),
t<tA[nops(tA)],Lag(t,tA[nops(tA)-2..nops(tA)],kA[nops(kA)-2..nops(kA)]),
kA[nops(kA)])),t,op(kA)):
```

```
beta:=(t,k2a,k2b,k2c)->piecewise(t<60,k2a,t<97,Lag(t,[60,80,97],[k2a,k2b,k2c]),k2c):
beta:=unapply(simplify(evalf(beta(t,k2a,k2b,k2c))),t,k2a,k2b,k2c):
```

```
EQS:=[op(Eqs),op(init)]:
```

```
res:=dsolve(EQS,numeric,map(q->q(t),v),output=listprocedure,parameters=par); assign('v[i]=subs
(res,v[i](t))' $ i=1..nops(v)):
```

```
chi2a:='chi2a': chi2:=unapply(chi2a(x0,xx,kA,x2a,x2b,x2c,x3),x0,xx,op(kA),x2a,x2b,x2c,x3):
```

```
chi2a:=proc(x0,xx,x1,x2a,x2b,x2c,x3) local i; global K; K:=xx;
res(parameters=[corr(par,[x0,xx,op(x1),x2a,x2b,x2c,x3])]):
sum((T[i]-K-A(i+dd))^2/(K-A(i+dd)),i=1..nops(T))+
sum((T2[i]-B(i+dd))^2/B(i+dd),i=1..nops(T2))+
sum((T3[i]-Q(i+dd))^2/Q(i+dd),i=1..nops(T2))+
sum((T1[i]-C(i+dd))^2/C(i+dd),i=1..nops(T1));
end:
```

```

chi2(op(pr(val))); val:=findMin(chi2,val); chi2(op(%));

#plot(map(q->q(t),v), t=0..3.0e4, legend=[``,``,``],
#linestyle=[solid,dash,dashdot],gridlines=true);

writedata(cat(Region,`3c.txt`),val);

display(
plot(map(q->q(t),v[1..3]), t=0..300, legend=[``,``,``],
linestyle=[solid,dash,dashdot],gridlines=true),
plot([[seq([i+dd,K_T[i]],i=1..nops(T))]],style=point,symbolsize=7,symbol=asterisk),
plot([[seq([i+dd,T1[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),
plot([[seq([i+dd,T2[i]],i=1..nops(T2))]],style=point,symbolsize=7,symbol=diamond,color=black),
size=[1000,400],legendstyle=[font=[roman,15]]
): fdisplay(cat(Region,`3c`),%);

```

$$\beta := (t, k2a, k2b, k2c) \mapsto \begin{cases} & k2a \\ (-0.2391891892 \cdot t + 0.001351351352 \cdot t^2 + 10.48648649) \cdot k2a + (-17.11764706 + 0.4617647058 \cdot t - 0.00294117647 \\ & k2c \end{cases}$$

```
res := [t=proc(t) ... end proc, A(t)=proc(t) ... end proc, B(t)=proc(t) ... end proc, C(t)=proc(t) ... end proc, Q(t)=proc(t)
```

```
...
```

```
end proc]
```

```
[9.027883628, 11843.41478, 0.05118252549, 0.08768869384, 0.1219317768, 0.1656771227, 0.1287578269, 0.1090075711, 0.08241319677,
0.3761057629, 0.01199523996, 0.1086118749, 0.2274905321, 0.0002732039562]
```

```
10872.1606133571
```

```
10872.1606133571
```

```
7551.74437593237
```

```
5834.01777657904
```

4894.49347302921  
4328.72078261343  
3972.40929033921  
3742.19902976995  
3578.38305200649  
3461.36389836751  
3373.66756069492  
3308.17216421439  
3252.46749149908  
3209.23462001351  
3169.57656973269  
3138.51428321800  
3109.78174622437  
3086.68871850301  
3066.01106213860  
3049.09345040577  
3032.52101463438  
3018.24086181784  
3004.26841455072  
2992.81933277276  
2976.80133296253  
2963.92810331168  
2949.86868578238  
2938.48329500879  
2924.78395782129  
2913.01451362374  
2889.36621973267  
2871.31594494162  
2797.93549245188  
2779.56038500471

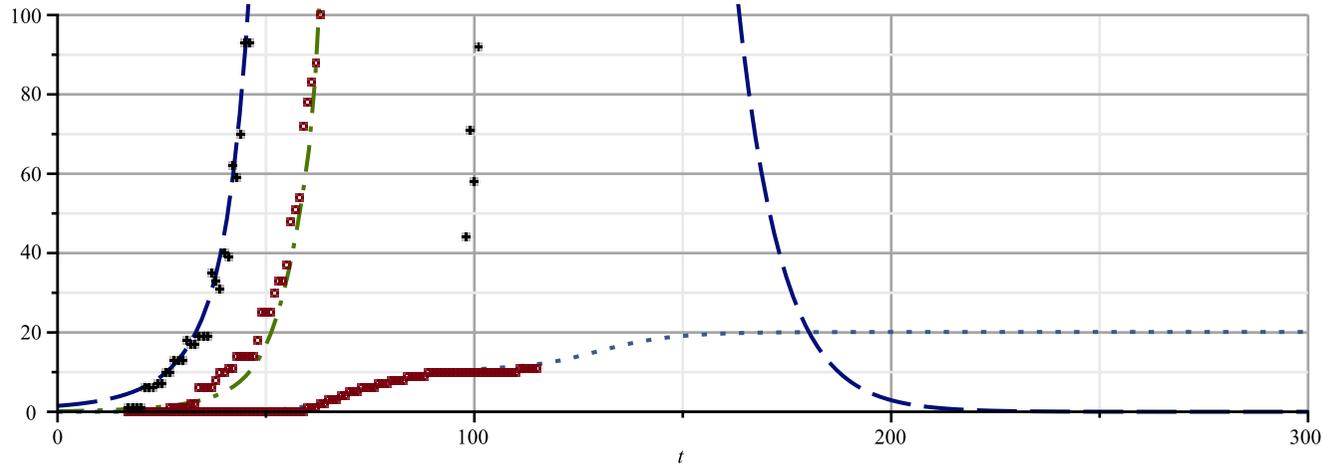
2772.26228017085  
2769.68188892357  
2736.64907345667  
2734.52349400282  
2732.73721075222  
2730.75325641776  
2729.14693674958  
2727.35120864736  
2725.93126104101  
2723.51190802225  
2721.69998430062  
2720.38995867076  
2719.30465172186  
2718.06045296415  
2717.04142312877  
2715.24127330503  
2713.69447654457  
2705.06004708067  
2700.40316525403  
2695.14502414509  
2694.00104861491  
2693.04355808238  
2692.58282247785  
2692.03413372638  
2691.63797319429  
2691.21791748518  
2690.88467037930  
2690.52197912210  
2690.21865884191  
2689.85639227305

2689.57497038410  
2688.26451624129  
2687.16117130984  
2680.30239825666  
2674.58406930313  
2671.39854758006  
2670.59238433451  
2670.11098668886  
2669.56867147283  
2669.25985638589  
2668.76843908993  
2668.42113131228  
2668.02412818297  
2667.68694231610  
2667.14444013638  
2666.72152403930  
2666.31937784936  
2665.98695199460  
2660.11898878064  
2654.77907719529  
2646.88531524702  
2643.13281172765  
2640.37225672826  
2639.73600258535  
2632.13441438392  
2629.69561861517  
2628.45309918324  
2627.44013737369  
2626.90619091041  
2626.38347835418



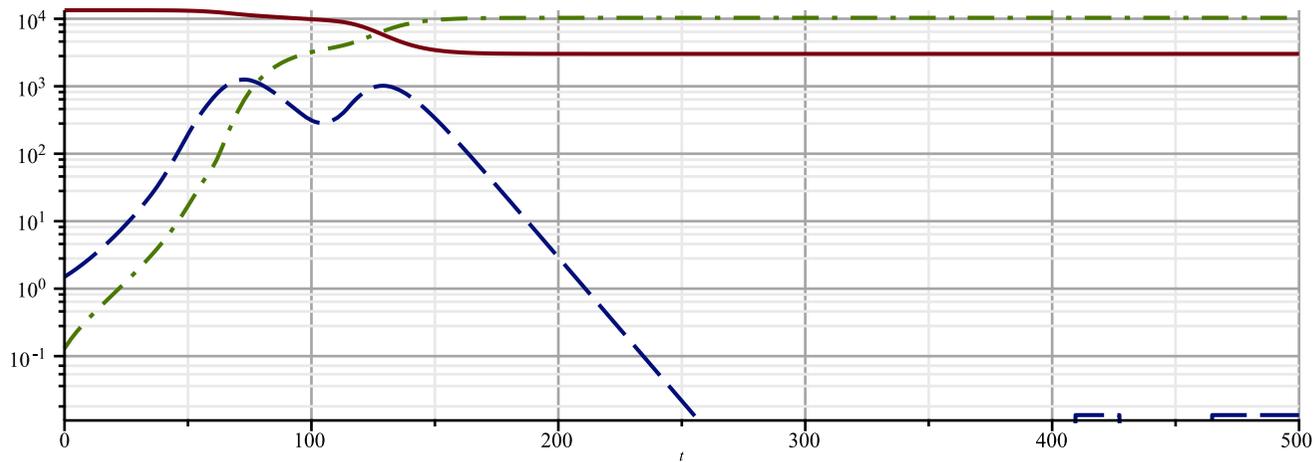
0.203563558116982, 0.000270413162241497]

2625.47158283574



— неинфицированные — больные - · - переболевшие · · · умершие

```
> logplot(map(q->q(t),v[1..3]),t=0..500,legend=[' ',' ',' ',' '],  
linestyle=[solid,dash,dashdot],gridlines=true,size=[1000,400],legendstyle=[font=[roman,15]]);
```



— неинфицированные — больные - · - переболевшие

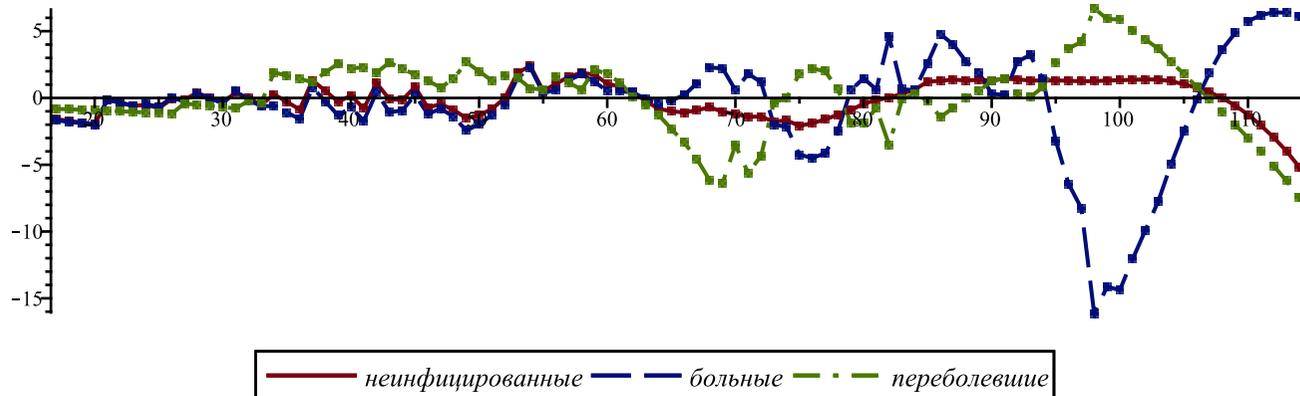
```
> display(  
plot([
```

```

[[i, (T[i-dd] - (K - A(i))) / sigma(K - A(i))] $ i=1+dd..dd+nops(T)],
[[i, (T2[i-dd] - (B(i))) / sigma(B(i))) $ i=1+dd..dd+nops(T)],
[[i, (T1[i-dd] - (C(i))) / sigma(C(i))] $ i=1+dd..dd+nops(T)]
], linestyle=[solid,dash,dashdot], legend = [ '\` , '\` , '\` ]
),
plot([
[[i, (T[i-dd] - (K - A(i))) / sigma(K - A(i))] $ i=1+dd..dd+nops(T)],
[[i, (T2[i-dd] - (B(i))) / sigma(B(i))) $ i=1+dd..dd+nops(T)],
[[i, (T1[i-dd] - (C(i))) / sigma(C(i))] $ i=1+dd..dd+nops(T)]
], style=point, symbolsize=8, symbol=solidcircle),
size=[1000,300], legendstyle=[font=[roman,15]]
): fdisplay(cat(Region, `3c-dev`), %);

```

RT3c-dev.jpg



```

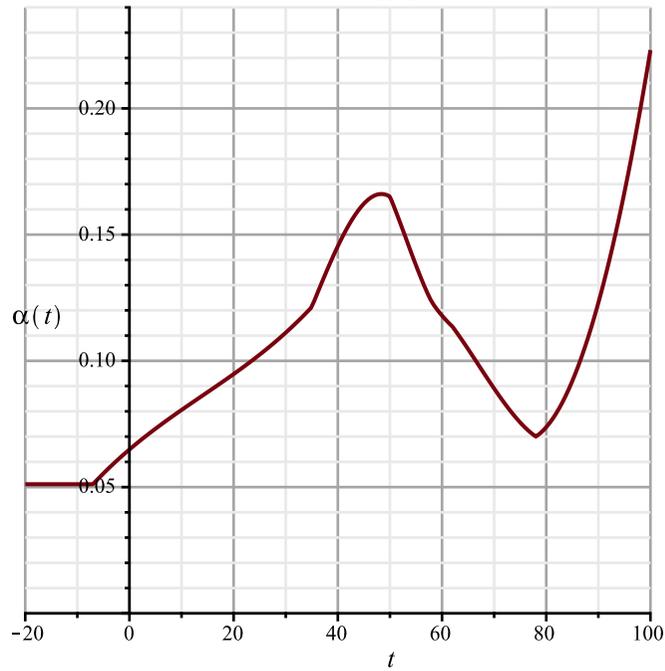
> [seq([i, (
(T[i-dd] - T[i-dd-1]) / (T2[i-dd] + T2[i-dd-1]) / ((1 - T[i-dd] / K_) + (1 - T[i-dd-1] / K_))
) * 4], i=1+dd+1..nops(T)+dd)]: [seq([%[i][1], (%[i-1][2] + %[i][2] + %[i+1][2]) / 3], i=2..nops(%)-1)]:
Palpha:=display(plot([%], color=blue), plot([%], style=point, symbolsize=8, symbol=solidcircle, color=
blue)):
#display(% , gridlines=true, labels=['t', 'alpha(t)'], labelfont=[roman,15], view=[0..nops(T)+dd, 0.
.0.9]);

subs(corr(par, val), alpha(t, op(kA)));
plot(% , t=-20..100, gridlines=true, labels=['t', 'alpha(t)'], labelfont=[roman,15], view=[-20..100, 0.
.0.24]):
fdisplay(cat(Region, `3c-zar`), %); display([Palpha, %], title = '\` , '\` , '\` ', titlefont=
[roman,20]);

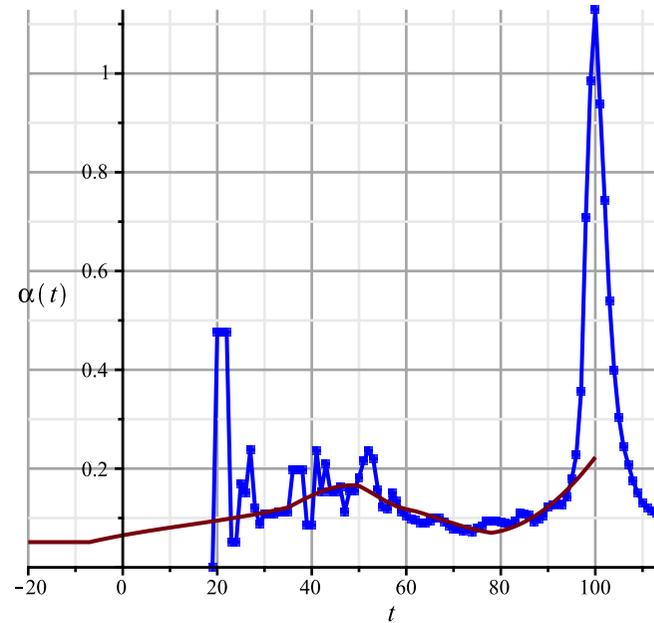
```

	$0.0511516341122043$	$t < -7.$
}	$6.04530802773049 \cdot 10^{-7} t^3 - 0.0000253186416718938 t^2 + 0.00175763078808757 t + 0.0649030171283571$	$t < 35.$
	$-9.03204975892332 \cdot 10^{-6} t^3 + 0.000938339415512518 t^2 - 0.0273930254385119 t + 0.317863257179106$	$t < 50.$
	$0.0000215906685086941 t^3 - 0.00344070930944677 t^2 + 0.177166733029866 t - 2.79034264888937$	$t < 58.$
	$-8.68422351596605 \cdot 10^{-6} t^3 + 0.00170602235274439 t^2 - 0.113351131958020 t + 2.65308294416811$	$t < 62.$
	$4.70513200205594 \cdot 10^{-6} t^3 - 0.000945070046235592 t^2 + 0.0601213589315806 t - 1.10247062461386$	$t < 78.$
	$0.000254738612732159 t^2 - 0.0383852845501610 t + 1.51424149384334$	$t < 115.$
	$0.468851923809304$	$115. \leq t$

*RT3c-zar.jpg*



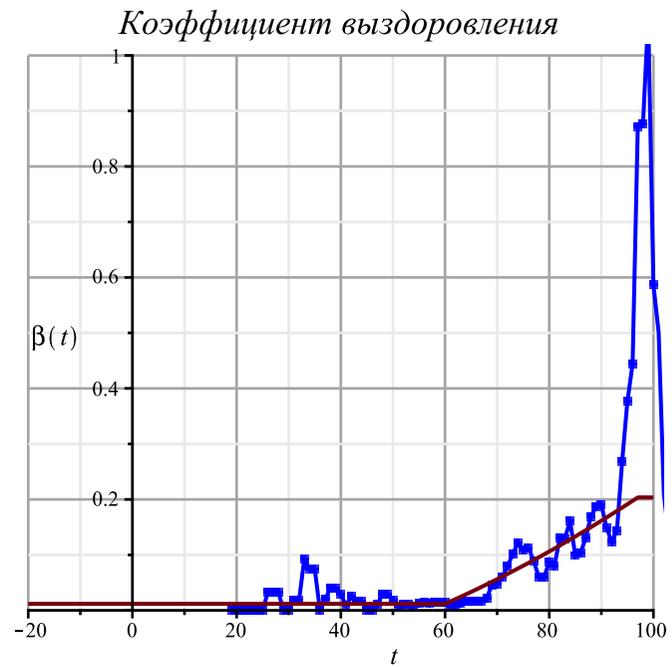
### Коэффициент заражения



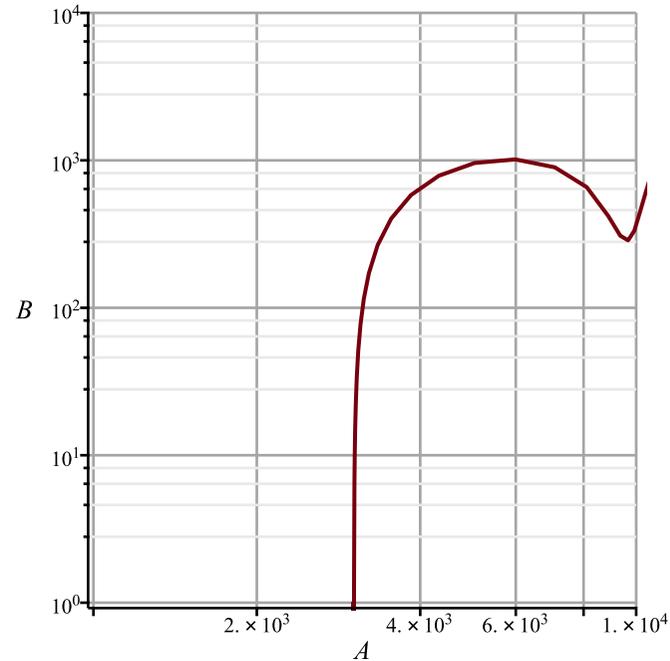
```
> [seq([i, (
    (T1[i-dd]-T1[i-dd-1]) / (T2[i-dd]+T2[i-dd-1])
)*2],i=1+dd+1..nops(T1)+dd)]: [seq([%[i][1], (%[i-1][2]+ %[i][2]+ %[i+1][2])/3],i=2..nops(%)-1)]:
Pbeta:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):

subs(corr(par,val),beta(t,k2a,k2b,k2c));
plot(%,t=-20..100,gridlines=true,labels=['t','beta(t)'],labelfont=[roman,15]):
display([Pbeta,%],t i t l e = ` ` ,titlefont=[roman,20],view=[-20..100,0..1]);
```

$$\left\{ \begin{array}{ll} 0.0117865640917915 & t < 60. \\ 0.000883945449305763 t + 0.0000273835447400681 t^2 - 0.139830925434023 & t < 97. \\ 0.203563558116982 & 97. \leq t \end{array} \right.$$



```
> plot([v[1](t),v[2](t),t=0..3.0e4],axis[1]=[mode=log],axis[2]=[mode=log],labels=[v[1],v[2]],
labelfont=[roman,15],gridlines=true,view=[10^3..10^4,10^0..10^4]);
```



```
> res:=solve(map(rhs,eqs[1..2]),v[1..2]); res:=res[2]; evalf(subs(param,t=100,res));
```

```
J:=Matrix(subs(res,map(q->grad(rhs(q),v[1..2]),eqs[1..2]))); J:=evalf(subs(param,corr(par,val),t=100,J));
```

```
evalm(%-lambda): collect(Determinant(%),lambda);
```

```
#evalf(subs(param,corr(par,val),t=100,%));
```

```
solve(%,{lambda});
```

$$res := \left[ \left[ A = \frac{C P_{01}}{P_{10} - P_{01}}, B = 0 \right], \left[ A = \frac{k0 (P_{23} + P_{20})}{P_{12}}, B = \frac{C P_{01} P_{12} + k0 P_{01} P_{20} + k0 P_{01} P_{23} - k0 P_{10} P_{20} - k0 P_{10} P_{23}}{P_{12} (P_{23} + P_{20})} \right] \right]$$

$$res := \left[ A = \frac{k0 (P_{23} + P_{20})}{P_{12}}, B = \frac{C P_{01} P_{12} + k0 P_{01} P_{20} + k0 P_{01} P_{23} - k0 P_{10} P_{20} - k0 P_{10} P_{23}}{P_{12} (P_{23} + P_{20})} \right]$$

$$\left[ A = \frac{k0 (k2c + k3)}{-0.38915095 klx6 + 0.96283784 klx7 + 0.426313107 klx8}, B = 0. \right]$$

$$J := \begin{bmatrix} P_{01} - \frac{C P_{01} P_{12} + k_0 P_{01} P_{20} + k_0 P_{01} P_{23} - k_0 P_{10} P_{20} - k_0 P_{10} P_{23}}{(P_{23} + P_{20}) k_0} & -P_{10} & -P_{23} & -P_{20} \\ \frac{C P_{01} P_{12} + k_0 P_{01} P_{20} + k_0 P_{01} P_{23} - k_0 P_{10} P_{20} - k_0 P_{10} P_{23}}{(P_{23} + P_{20}) k_0} & & & 0 \end{bmatrix}$$

$$J := \begin{bmatrix} 0. & -0.203833971279223 \\ 0. & 0. \end{bmatrix}$$

$$\lambda^2$$

$$\{\lambda=0\}, \{\lambda=0\}$$

(9)

```
> N:='N': A:='A': B:='B': C:='C': Q:='Q':
```

```
param:=[
  P[`01`] = kappa, P[`12`] = k1, P[`23`] = k2,
  P[`10`] = kappa, P[`20`] = k3, P[`30`] = k4
];
corr(par, val);
subs(param, eqs); R:=solve(% , [k1, k2, k3, k4]) [1];
```

```
X:='X': X1:='X1': subs(R, Diff(A, t) = -X1[1][i][2], Diff(B, t) = X1[2][i][2], Diff(C, t) = X1[3][i][2], Diff
(Q, t) = X1[4][i][2], A = k0 - X[1][i][2], B = X[2][i][2], C = X[3][i][2], Q = X[4][i][2], [k1, k2, k3, k4]): XX:=
unapply(subs(k0=K_, %), i):
```

$$param := [P_{01} = 0, P_{12} = k1, P_{23} = k2, P_{10} = 0, P_{20} = k3, P_{30} = k4]$$

```
d0 = 9.04975926871991, k0 = 13380.7013637885, k1x1 = 0.0511516341122043, k1x2 = 0.0876110760233198, k1x3 = 0.121324016958117,
k1x4 = 0.165054303003467, k1x5 = 0.123380281215598, k1x6 = 0.113569079033557, k1x7 = 0.0700190187615531, k1x8
= 0.468851923809304, k2a = 0.0117865640917915, k2b = 0.106139398901217, k2c = 0.203563558116982, k3 = 0.000270413162241497
```

$$\left[ \frac{\partial}{\partial t} A = -\frac{B k1 A}{k0}, \frac{\partial}{\partial t} B = \frac{B k1 A}{k0} - k2 B - k3 B, \frac{\partial}{\partial t} C = k2 B - C k4, \frac{\partial}{\partial t} Q = k3 B \right]$$

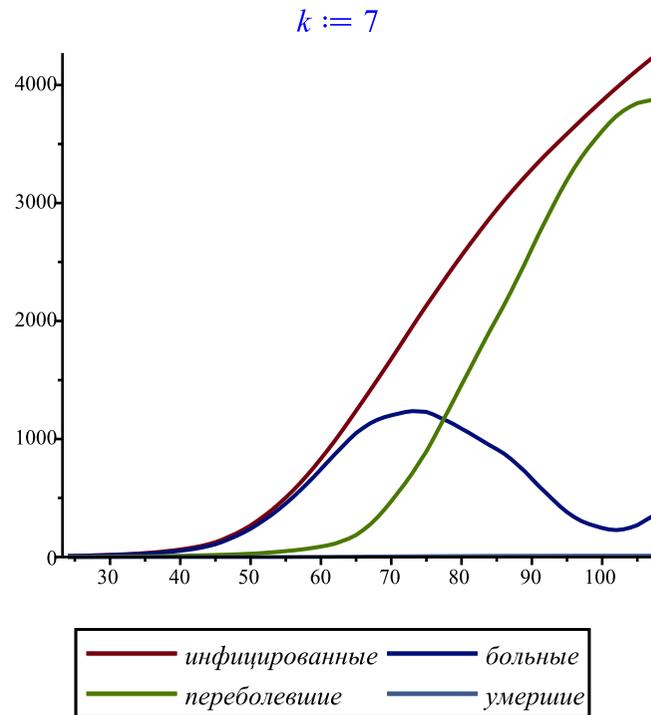
(10)

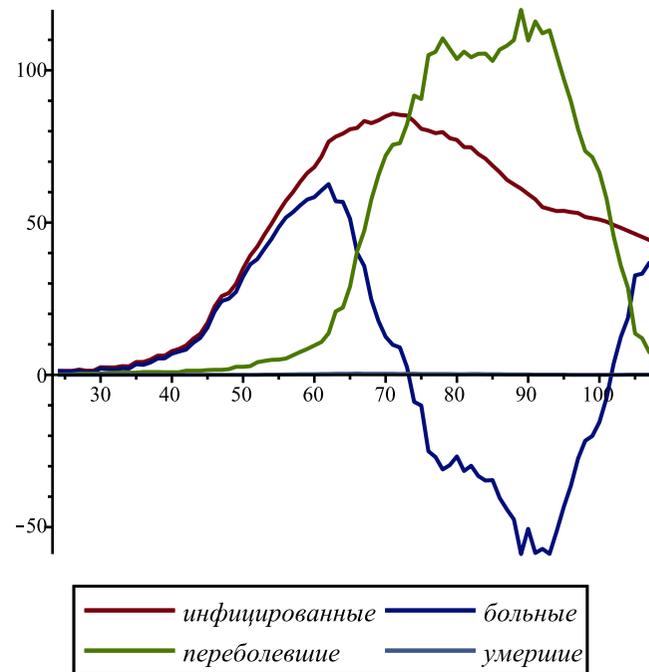
$$R := \left[ k1 = -\frac{\frac{\partial}{\partial t} A k0}{AB}, k2 = -\frac{\frac{\partial}{\partial t} B + \frac{\partial}{\partial t} Q + \frac{\partial}{\partial t} A}{B}, k3 = \frac{\frac{\partial}{\partial t} Q}{B}, k4 = -\frac{\frac{\partial}{\partial t} B + \frac{\partial}{\partial t} Q + \frac{\partial}{\partial t} A + \frac{\partial}{\partial t} C}{C} \right] \quad (10)$$

```

> k:=7;
X:=map(q->[seq([i+dd, (ssum(q[i+j], j=-k..k)) / (2*k)], i=1+k..nops(q)-k)], [T, T2, T1, T3]):
plot(%, legend=[' ', ' ', ' ', ' '], legendstyle=[font=[roman, 15]]);
X1:=map(q->[seq([i+dd, (q[i+k]-q[i-k]) / (2*k)], i=1+k..nops(q)-k)], [T, T2, T1, T3]):
plot(%, legend=[' ', ' ', ' ', ' '], legendstyle=[font=[roman, 15]]);
);

```





> k:=0;

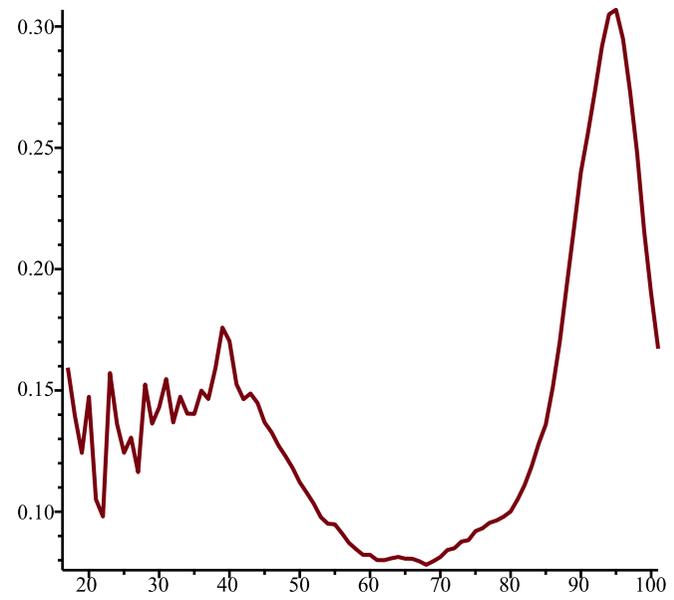
```
[seq([i+dd+k,XX(i)[1]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`12`],titlefont=[roman,20]);
```

```
[seq([i+dd+k,XX(i)[2]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`23`],titlefont=[roman,20]);
```

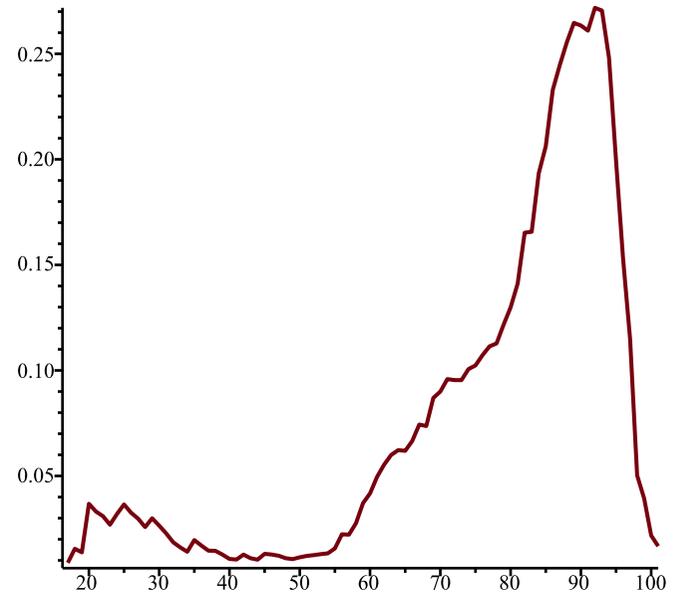
```
[seq([i+dd+k,XX(i)[3]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`20`],titlefont=[roman,20]);
```

k := 0

$P_{12}$



$P_{23}$



$P_{20}$

