

```

> restart;
with(plots):
with(StringTools):
with(LinearAlgebra):
with(DEtools):

#####

Region:='Mosobl'; url:="https://gogov.ru/covid-19/mo#data";

#valp := [12.0545284599666, 40487.7036090492, 0.0878540675828671, 0.119034763474605,
0.208571881538399, 0.163876229453231, #0.0804863589181470, 0.0940935501988715, 0.105057419991328,
0.104244846871936, 0.00441107479765352, 0.00987259141378349, #0.0000931839501779284];

valp:=readdata(cat(Region,`3c.txt`));
#valp:=[13.51351539, 60412.96696, 0.1007399931, 0.1125440131, 0.2130928266, 0.1556319126,
0.07614930869, 0.07804499825, #0.07915349053, 0.1233558069, 0.007192627605, 0.00339175117,
0.01641051065, 0.0006085575277];

#####

fdisplay:=proc(f,p)
print(cat(f,`.jpg`)); #print(cat(f,`.eps`));
plotsetup(jpeg,plotoutput=cat(f,`.jpg`),plotoptions=`noborder`); print(display(p));
plotsetup(ps,plotoutput=cat(f,`.eps`),plotoptions=`noborder`); print(display(p));
plotsetup(default,plotoptions=`noborder`): print(display(p));
end:

pr:=proc(x) print(x); x; end:

grad:=(F,V)->map(q->diff(F,q),V):

linsplit:=(F,V)->subs(map(q->q=0,V),[op(grad(F,V)),F]):

corr:=proc(x,y) local i; seq(x[i]=y[i],i=1..nops(x)): end:

ssum:=(F,V)->convert([seq(F,V)],`+`):

pprod:=(F,V)->convert([seq(F,V)],`*`):

```

```

Lag:=proc(t,tx,kx) local i,j;
  ssum(kx[i]*pprod(piecewise(j=i,1,(t-tx[j])/(tx[i]-tx[j])),j=1..nops(tx)),i=1..nops(tx)):
end:

```

```

Lag(t,[ta,tb],[a,b]); Lag(t,[ta,tb,tc],[a,b,c]);

```

```

pi:=evalf(Pi);

```

```

gM:=evalf(solve((1-x)^2=x,x)[2]):
goldMin:=proc(f,T,epsilon) local a,b,c,d,fa,fb,fc,fd,k;
  a:=op(1,T); b:=op(2,T); fa:=f(a); fb:=f(b); k:=0;
  c:=a+(b-a)*gM; fc:=f(c); d:=b-(b-a)*gM; fd:=f(d);
  while abs(a-b)>epsilon do: k:=k+1;
    if fc>fd then a:=c; fa:=fc; c:=d; fc:=fd; d:=b-(b-a)*gM; fd:=f(d);
    else b:=d; fb:=fd; d:=c; fd:=fc; c:=a+(b-a)*gM; fc:=f(c);
    fi;
  od: #print(k);
  (a+b)/2;
end:

```

```

findMin1:=proc(F,V) local f,df,f0,f1,f2,V0,V1,V2,ff,t,dt,i,j;
  ff:=V->F(op(evalf(map(exp,V)))); V1:=evalf(map(ln,V)); f1:=F(op(V));
  f:=[seq(F(seq(evalf(exp(V1[j]+piecewise(j=i,0.0001,0))),j=1..nops(V))),i=1..nops(V))];
  df:=[seq((f[j]-f1)/0.1,j=1..nops(V))];
  V0:=V1-0.001*df; f0:=ff(V0); V2:=V1+0.001*df; f2:=ff(V2);
  dt:=0.0001; while f0<f1 do: V2:=V1; f2:=f1; V1:=V0; f1:=f0; V0:=V0-dt*df; f0:=ff(V0); dt:=dt*
  1.5; od;
  dt:=0.0001; while f2<f1 do: V0:=V1; f0:=f1; V1:=V2; f1:=f2; V2:=V2+dt*df; f2:=ff(V2); dt:=dt*
  1.5; od;
  t:=goldMin(t->ff(t*V0+(1-t)*V2),0..1,0.001);
  map(exp,t*V0+(1-t)*V2);
end:

```

```

findMin:=proc(F,V) local V1,Z1,Z2;
  Z2:=pr(F(op(V))); V1:=findMin1(F,V); Z1:=pr(chi2(op(V1)));
  while abs(1-Z1/Z2)>0.0001 do: Z2:=Z1; V1:=findMin1(F,V1); Z1:=pr(chi2(op(V1))); end;
  V1;
end:

```

Region := Mosobl

url := "https://gogov.ru/covid-19/mo#data"

valp := [13.44258404, 62802.67494, 0.1012133281, 0.1111242458, 0.2115507857, 0.1595470238, 0.08751331813, 0.08130220975, 0.07749483653, 0.1277152111, 0.007412379613, 0.01037824493, 0.0236434147, 0.0006037801923]

$$\frac{a(t-tb)}{ta-tb} + \frac{b(t-ta)}{tb-ta}$$
$$\frac{a(t-tb)(t-tc)}{(ta-tb)(ta-tc)} + \frac{b(t-ta)(t-tc)}{(tb-ta)(tb-tc)} + \frac{c(t-ta)(t-tb)}{(tc-ta)(tc-tb)}$$
$$\pi := 3.141592654$$

(1)

```
> dig:={"0","1","2","3","4","5","6","7","8","9","0"}: val:=proc() global data,i; local j,f; f:=0;
  while not(data[i] in dig) or f=1 and data[i] in {"+"} union dig do:
  if f=1 and not(data[i] in dig) then f:=0; else if data[i]="+" then f:=1; fi fi; i:=i+1: od:
  j:=i; while (data[i] in dig or data[i] in {"-","+"}) do i:=i+1: od: parse(data[j..i-1]);
end:
` `; Region; status,data,headers:=HTTP:-Get(url): HTTP:-Code(status); i:=Search("<th>",data):

iter:=proc() global i; local r;
  r:=val(); if data[i]<>"." then NULL else [r,val(),val(),val(),val(),val()],iter() fi;
end:

[iter()]: tA:=seq(%[nops(%)+1-i],i=1..nops(%));
dd:=tA[1][1]+piecewise(tA[1][2]=2,-29,tA[1][2]=4,31,0)-1;
T:=map(q->q[4],tA): #writedata(Region || `-i.txt`,%): #
T3:=map(q->q[5],tA): #writedata(Region || `-m.txt`,%): #
T1:=map(q->q[6],tA): #writedata(Region || `-r.txt`,%): #
T2:=seq(T[i]-(T1[i]+T3[i]),i=1..nops(T)): #writedata(Region || `-h.txt`,%): #
i:='i':
Region; 'T'=T; 'T1'=T1; 'T2'=T2; 'T3'=T3;

nops(T); [i+dd $ i=1..%];
```

Mosobl

"OK"

tA := [[8, 3, 20, 1, 0, 0], [9, 3, 20, 1, 0, 0], [10, 3, 20, 1, 0, 0], [11, 3, 20, 3, 0, 0], [12, 3, 20, 3, 0, 0], [13, 3, 20, 4, 0, 0], [14, 3, 20, 5, 0, 0],

[15, 3, 20, 8, 0, 0], [16, 3, 20, 9, 0, 0], [17, 3, 20, 11, 0, 0], [18, 3, 20, 12, 0, 0], [19, 3, 20, 17, 0, 0], [20, 3, 20, 18, 0, 1], [21, 3, 20, 35, 0, 1], [22, 3, 20, 35, 0, 1], [23, 3, 20, 35, 0, 1], [24, 3, 20, 35, 0, 2], [25, 3, 20, 41, 0, 7], [26, 3, 20, 41, 0, 7], [27, 3, 20, 49, 0, 8], [28, 3, 20, 85, 0, 8], [29, 3, 20, 112, 0, 10], [30, 3, 20, 119, 0, 10], [31, 3, 20, 119, 0, 14], [1, 4, 20, 134, 1, 17], [2, 4, 20, 177, 2, 17], [3, 4, 20, 211, 2, 17], [4, 4, 20, 260, 2, 30], [5, 4, 20, 305, 2, 33], [6, 4, 20, 387, 3, 34], [7, 4, 20, 454, 8, 47], [8, 4, 20, 549, 10, 50], [9, 4, 20, 748, 13, 52], [10, 4, 20, 930, 13, 66], [11, 4, 20, 1082, 14, 69], [12, 4, 20, 1360, 18, 75], [13, 4, 20, 1855, 19, 75], [14, 4, 20, 2315, 24, 75], [15, 4, 20, 2587, 26, 75], [16, 4, 20, 3054, 33, 91], [17, 4, 20, 3526, 40, 105], [18, 4, 20, 3954, 40, 126], [19, 4, 20, 4663, 49, 162], [20, 4, 20, 5241, 49, 176], [21, 4, 20, 5959, 49, 179], [22, 4, 20, 6590, 56, 186], [23, 4, 20, 7278, 56, 186], [24, 4, 20, 7889, 66, 235], [25, 4, 20, 8494, 69, 262], [26, 4, 20, 9070, 71, 272], [27, 4, 20, 9708, 71, 286], [28, 4, 20, 10231, 74, 311], [29, 4, 20, 10917, 90, 389], [30, 4, 20, 11710, 93, 430], [1, 5, 20, 12507, 109, 458], [2, 5, 20, 13314, 109, 503], [3, 5, 20, 14136, 111, 507], [4, 5, 20, 14939, 111, 526], [5, 5, 20, 15761, 127, 576], [6, 5, 20, 16590, 141, 611], [7, 5, 20, 17432, 156, 769], [8, 5, 20, 18350, 175, 813], [9, 5, 20, 19425, 186, 1030], [10, 5, 20, 20558, 195, 1236], [11, 5, 20, 21637, 209, 1389], [12, 5, 20, 22700, 219, 1582], [13, 5, 20, 23662, 226, 1745], [14, 5, 20, 24580, 240, 1987], [15, 5, 20, 25525, 253, 2468], [16, 5, 20, 26462, 262, 2724], [17, 5, 20, 27369, 268, 3088], [18, 5, 20, 28290, 268, 3361], [19, 5, 20, 29188, 271, 3614], [20, 5, 20, 30091, 285, 3897], [21, 5, 20, 30983, 299, 4281], [22, 5, 20, 31807, 312, 4699], [23, 5, 20, 32653, 324, 5163], [24, 5, 20, 33515, 329, 5520], [25, 5, 20, 34346, 340, 5908], [26, 5, 20, 35163, 349, 6152], [27, 5, 20, 35956, 359, 6440], [28, 5, 20, 36730, 380, 6843], [29, 5, 20, 37503, 400, 7333], [30, 5, 20, 38238, 424, 7720], [31, 5, 20, 38995, 449, 8091], [1, 6, 20, 39723, 473, 8422], [2, 6, 20, 40455, 495, 8809], [3, 6, 20, 41191, 515, 9311], [4, 6, 20, 41958, 534, 9877], [5, 6, 20, 42720, 539, 10392], [6, 6, 20, 43478, 557, 10924], [7, 6, 20, 44232, 567, 11462], [8, 6, 20, 44983, 578, 12031], [9, 6, 20, 45722, 590, 12672], [10, 6, 20, 46457, 622, 13419], [11, 6, 20, 47181, 644, 14187], [12, 6, 20, 47911, 666, 14955], [13, 6, 20, 48636, 678, 15734], [14, 6, 20, 49353, 678, 16573], [15, 6, 20, 50042, 690, 17422], [16, 6, 20, 50736, 702, 18340], [17, 6, 20, 51416, 728, 19319], [18, 6, 20, 52083, 751, 20355], [19, 6, 20, 52729, 755, 21448], [20, 6, 20, 53320, 778, 22596], [21, 6, 20, 53869, 783, 23798], [22, 6, 20, 54375, 783, 25036], [23, 6, 20, 54879, 798, 26198]]

dd := 7

Mosobl

T = [1, 1, 1, 3, 3, 4, 5, 8, 9, 11, 12, 17, 18, 35, 35, 35, 35, 41, 41, 49, 85, 112, 119, 119, 134, 177, 211, 260, 305, 387, 454, 549, 748, 930, 1082, 1360, 1855, 2315, 2587, 3054, 3526, 3954, 4663, 5241, 5959, 6590, 7278, 7889, 8494, 9070, 9708, 10231, 10917, 11710, 12507, 13314, 14136, 14939, 15761, 16590, 17432, 18350, 19425, 20558, 21637, 22700, 23662, 24580, 25525, 26462, 27369, 28290, 29188, 30091, 30983, 31807, 32653, 33515, 34346, 35163, 35956, 36730, 37503, 38238, 38995, 39723, 40455, 41191, 41958, 42720, 43478, 44232, 44983, 45722, 46457, 47181, 47911, 48636, 49353, 50042, 50736, 51416, 52083, 52729, 53320, 53869, 54375, 54879]

TI = [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 2, 7, 7, 8, 8, 10, 10, 14, 17, 17, 17, 30, 33, 34, 47, 50, 52, 66, 69, 75, 75, 75, 75, 91, 105, 126, 162, 176, 179, 186, 186, 235, 262, 272, 286, 311, 389, 430, 458, 503, 507, 526, 576, 611, 769, 813, 1030, 1236, 1389, 1582, 1745, 1987,


```

[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T))]: [seq((%[i]-%[i-3])/3.,i=4..nops(%))]: [seq((%[i]-%
[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=[``,``,``]),
  title = `          N [ i ]          `,titlefont=[roman,15],gridlines=true
);

```

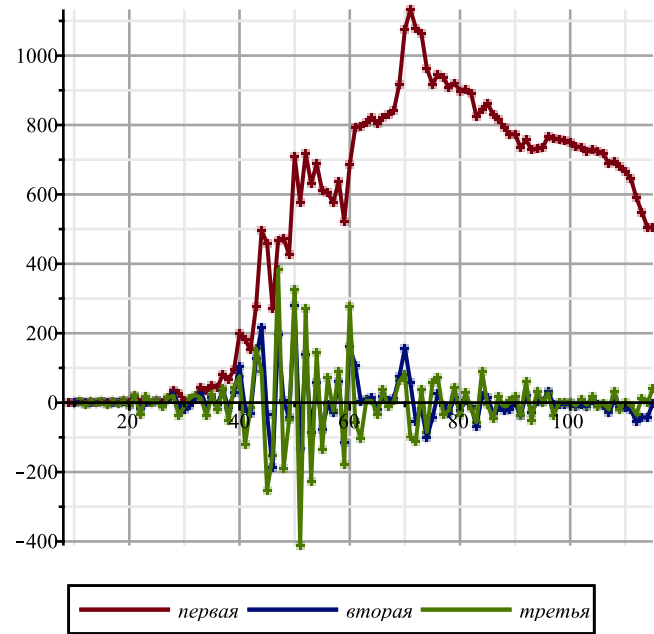
$$h := x \mapsto x$$

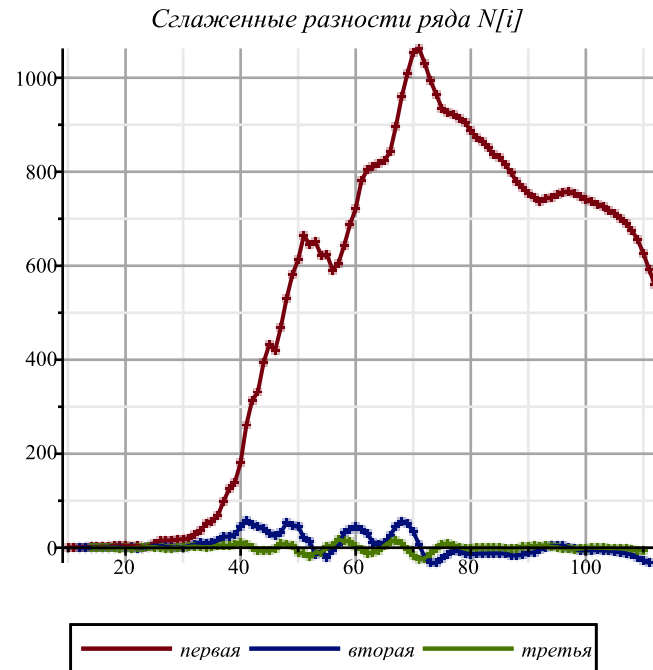
```

[0, 0, 2, 0, 1, 1, 3, 1, 2, 1, 5, 1, 17, 0, 0, 0, 6, 0, 8, 36, 27, 7, 0, 15, 43, 34, 49, 45, 82, 67, 95, 199, 182, 152, 278, 495, 460, 272, 467, 472, 428,
709, 578, 718, 631, 688, 611, 605, 576, 638, 523, 686, 793, 797, 807, 822, 803, 822, 829, 842, 918, 1075, 1133, 1079, 1063, 962, 918, 945,
937, 907, 921, 898, 903, 892, 824, 846, 862, 831, 817, 793, 774, 773, 735, 757, 728, 732, 736, 767, 762, 758, 754, 751, 739, 735, 724, 730,
725, 717, 689, 694, 680, 667, 646, 591, 549, 506, 504]
[0, 2, -2, 1, 0, 2, -2, 1, -1, 4, -4, 16, -17, 0, 0, 6, -6, 8, 28, -9, -20, -7, 15, 28, -9, 15, -4, 37, -15, 28, 104, -17, -30, 126, 217,
-35, -188, 195, 5, -44, 281, -131, 140, -87, 57, -77, -6, -29, 62, -115, 163, 107, 4, 10, 15, -19, 19, 7, 13, 76, 157, 58, -54,
-16, -101, -44, 27, -8, -30, 14, -23, 5, -11, -68, 22, 16, -31, -14, -24, -19, -1, -38, 22, -29, 4, 4, 31, -5, -4, -4, -3,
-12, -4, -11, 6, -5, -8, -28, 5, -14, -13, -21, -55, -42, -43, -2]
[2, -4, 3, -1, 2, -4, 3, -2, 5, -8, 20, -33, 17, 0, 6, -12, 14, 20, -37, -11, 13, 22, 13, -37, 24, -19, 41, -52, 43, 76, -121, -13,
156, 91, -252, -153, 383, -190, -49, 325, -412, 271, -227, 144, -134, 71, -23, 91, -177, 278, -56, -103, 6, 5, -34, 38, -12,
6, 63, 81, -99, -112, 38, -85, 57, 71, -35, -22, 44, -37, 28, -16, -57, 90, -6, -47, 17, -10, 5, 18, -37, 60, -51, 33, 0, 27,
-36, 1, 0, 1, -9, 8, -7, 17, -11, -3, -20, 33, -19, 1, -8, -34, 13, -1, 41]

```

Разности ряда $N[i]$





```
> h:=x->evalf(ln(x));
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=[``,``,``]),
  title=` ln(N[i])`,titlefont=[roman,15] ,gridlines=true
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%
[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=[``,``,``]),
```



```
title = `ln(N[i])`,titlefont=[roman,15],gridlines=true);
```

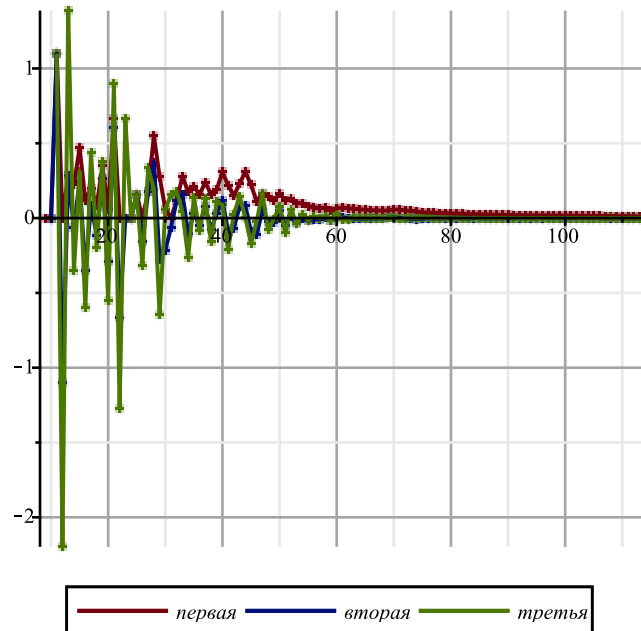
$h := x \mapsto \text{evalf}(\ln(x))$

```
[0., 0., 1.098612289, 0., 0.287682072, 0.223143551, 0.470003630, 0.117783036, 0.200670695, 0.087011377, 0.348306694, 0.057158414, 0.664976303, 0., 0., 0.158224006, 0., 0.178248231, 0.550830958, 0.275847615, 0.060624622, 0., 0.118716307, 0.278309933, 0.175708400, 0.208823498, 0.159630146, 0.238112916, 0.159672505, 0.190001244, 0.309304536, 0.217781608, 0.151381873, 0.228673520, 0.310399996, 0.221524992, 0.111089215, 0.165953304, 0.143711877, 0.114563641, 0.164931293, 0.116853302, 0.128390362, 0.100650666, 0.099302751, 0.080613285, 0.073890648, 0.065612232, 0.067978024, 0.052472039, 0.064898880, 0.070121971, 0.065845310, 0.062527625, 0.059908622, 0.055250508, 0.053563291, 0.051261570, 0.049507494, 0.051321976, 0.056931322, 0.056689264, 0.051154652, 0.047960109, 0.04150546, 0.03806272, 0.03772526, 0.03605138, 0.03370125, 0.03309739, 0.03124928, 0.03046846, 0.02921255, 0.02624772, 0.02625034, 0.02605637, 0.02449246, 0.02350883, 0.02230158, 0.02129789, 0.02082707, 0.01940885, 0.01960365, 0.01849693, 0.01825988, 0.01802954, 0.01844934, 0.01799807, 0.01758787, 0.01719345, 0.01683613, 0.01629494, 0.01594757, 0.01546412, 0.01535385, 0.01501888, 0.01463455, 0.01386410, 0.01377307, 0.01331369, 0.01288919, 0.01232699, 0.01114590, 0.01024368, 0.00934932, 0.00922627]
```

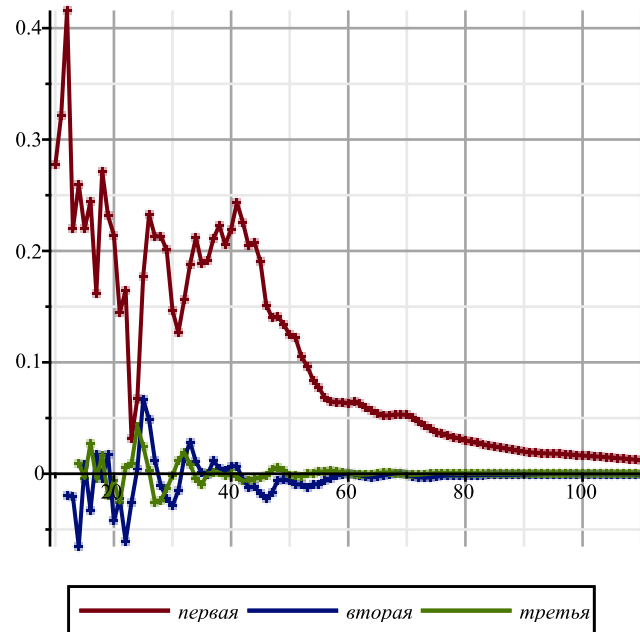
```
[0., 1.098612289, -1.098612289, 0.287682072, -0.064538521, 0.246860079, -0.352220594, 0.082887659, -0.113659318, 0.261295317, -0.291148280, 0.607817889, -0.664976303, 0., 0., 0.158224006, -0.158224006, 0.178248231, 0.372582727, -0.274983343, -0.215222993, -0.060624622, 0.118716307, 0.159593626, -0.102601533, 0.033115098, -0.049193352, 0.078482770, -0.078440411, 0.030328739, 0.119303292, -0.091522928, -0.066399735, 0.077291647, 0.081726476, -0.088875004, -0.110435777, 0.054864089, -0.022241427, -0.029148236, 0.050367652, -0.048077991, 0.011537060, -0.027739696, -0.001347915, -0.018689466, -0.006722637, -0.008278416, 0.002365792, -0.015505985, 0.012426841, 0.005223091, -0.004276661, -0.003317685, -0.002619003, -0.004658114, -0.001687217, -0.002301721, -0.001754076, 0.001814482, 0.005609346, -0.000242058, -0.005534612, -0.003194543, -0.006454649, -0.00344274, -0.00033746, -0.00167388, -0.00235013, -0.00060386, -0.00184811, -0.00078082, -0.00125591, -0.00296483, 2.62 10-6, -0.00019397, -0.00156391, -0.00098363, -0.00120725, -0.00100369, -0.00047082, -0.00141822, 0.00019480, -0.00110672, -0.00023705, -0.00023034, 0.00041980, -0.00045127, -0.00041020, -0.00039442, -0.00035732, -0.00054119, -0.00034737, -0.00048345, -0.00011027, -0.00033497, -0.00038433, -0.00077045, -0.00009103, -0.00045938, -0.00042450, -0.00056220, -0.00118109, -0.00090222, -0.00089436, -0.00012305]
```

[1.098612289, -2.197224578, 1.386294361, -0.352220593, 0.311398600, -0.599080673, 0.435108253, -0.196546977, 0.374954635, -0.552443597, 0.898966169, -1.272794192, 0.664976303, 0., 0.158224006, -0.316448012, 0.336472237, 0.194334496, -0.647566070, 0.059760350, 0.154598371, 0.179340929, 0.040877319, -0.262195159, 0.135716631, -0.082308450, 0.127676122, -0.156923181, 0.108769150, 0.088974553, -0.210826220, 0.025123193, 0.143691382, 0.004434829, -0.170601480, -0.021560773, 0.165299866, -0.077105516, -0.006906809, 0.079515888, -0.098445643, 0.059615051, -0.039276756, 0.026391781, -0.017341551, 0.011966829, -0.001555779, 0.010644208, -0.017871777, 0.027932826, -0.007203750, -0.009499752, 0.000958976, 0.000698682, -0.002039111, 0.002970897, -0.000614504, 0.000547645, 0.003568558, 0.003794864, -0.005851404, -0.005292554, 0.002340069, -0.003260106, 0.003011909, 0.00310528, -0.00133642, -0.00067625, 0.00174627, -0.00124425, 0.00106729, -0.00047509, -0.00170892, 0.00296745, -0.00019659, -0.00136994, 0.00058028, -0.00022362, 0.00020356, 0.00053287, -0.00094740, 0.00161302, -0.00130152, 0.00086967, $6.71 \cdot 10^{-6}$, 0.00065014, -0.00087107, 0.00004107, 0.00001578, 0.00003710, -0.00018387, 0.00019382, -0.00013608, 0.00037318, -0.00022470, -0.00004936, -0.00038612, 0.00067942, -0.00036835, 0.00003488, -0.00013770, -0.00061889, 0.00027887, $7.86 \cdot 10^{-6}$, 0.00077131]

Разности ряда $\ln(N[i])$



Сглаженные разности ряда $\ln(N[i])$



```

> f_:=d->sum(a[j]*d^j,j=0..n); fe_:=d->sum(a[j]*d^j,j=0..ne);

M:='M':
ff:=x->M*(1-1/(exp(x)+1)); ff_:=unapply(solve(y=ff(x),x),y); diff(ff_(x),x); dff_:=unapply
(simplify(% ,x),x);
ffe:=x->exp(x); ffe_:=unapply(solve(y=ffe(x),x),y); diff(ff_(x),x); dffe_:=unapply(simplify(% ,
x),x);

sigma:=x->simplify(sqrt(x));

chi2:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dff_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));
chi2e:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dffe_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));

F:=proc(T,chi2,f_) chi2(T,f_);
  indets(%); grad(% ,%); subs(solve(% ,%),f_(i)); unapply(% ,i);
end:

```

$$f_- := d \mapsto \sum_{j=0}^n a_j \cdot d^j$$

$$fe_- := d \mapsto \sum_{j=0}^{ne} a_j \cdot d^j$$

$$ff := x \mapsto M \cdot \left(1 - \frac{1}{e^x + 1} \right)$$

$$ff_- := y \mapsto \ln\left(\frac{y}{M-y}\right)$$

$$\frac{\left(\frac{1}{M-x} + \frac{x}{(M-x)^2} \right) (M-x)}{x}$$

$$dff_- := x \mapsto \frac{M}{(M-x) \cdot x}$$

$$ffe := x \mapsto e^x$$

$$ffe_- := y \mapsto \ln(y)$$

$$\frac{1}{x}$$

$$dffe_- := x \mapsto \frac{1}{x}$$

$$\sigma := x \mapsto \text{simplify}(\sqrt{x})$$

$$\chi^2 := (T, f_-) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ff_-(T_k) - f_-(k))^2}{dff_-(T_k)^2 \sigma(T_k)^2} \right)$$

$$\chi^2e := (T, f_-) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ffe_-(T_k) - f_-(k))^2}{dffe_-(T_k)^2 \sigma(T_k)^2} \right)$$

```
> n:=1: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);
```

```

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],
gridlines=true);

d1:=fsolve(f(d)=0.5*M,d=30)+dd; K_:=M; alpha_:=coeff(nu(t),t,1);

n:=4: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);

[seq([i,(
(T[i-dd]-T[i-dd-1])/(T2[i-dd]+T2[i-dd-1])/((1-T[i-dd]/M)+(1-T[i-dd-1]/M))
)*4],i=1+dd+1..nops(T)+dd)]: [seq([%[i][1],(%[i-1][2]+[%i][2]+[%i+1][2])/3],i=2..nops(%)-1)]:
Palpha:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],

```

```
gridlines=true) :
display(Palpha,%) ;
```

$$f(t) = \sum_{j=0}^1 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$M := 54881.42820$$

$$N(t) = 54881.42820 - \frac{54881.42820}{e^{0.08319143551 t - 5.950746677} + 1}$$

$$Chi2 := 21280.83471$$

Next day forecast: 52554

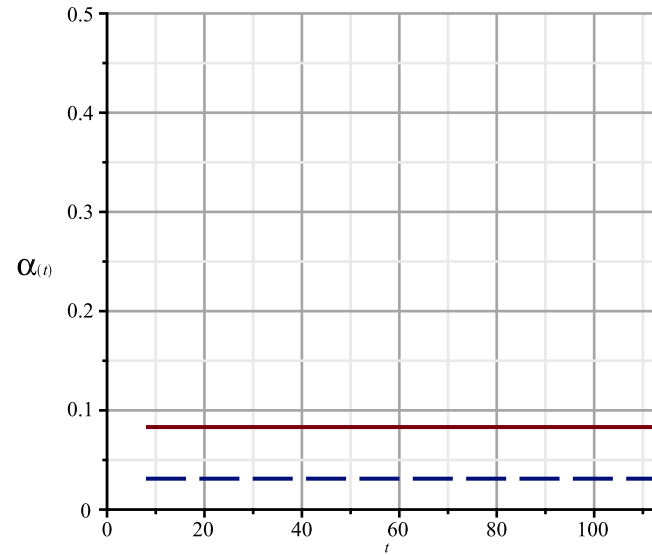
The level of 0.5 M is reached at 49 apr

The level of 0.85 M is reached at 69 apr

Approximation of the infection schedule by solving the Malthus equation

$$N(t) = e^{0.03117217699 t + 7.791741183} [0.08319143551]$$

Коэффициент заражения



— Ферхюльст - - - Мальтус

$$dI := 78.53076084$$

$$K_ := 54881.42820$$

$$alpha_ := 0.08319143551$$

$$f(t) = \sum_{j=0}^4 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$M := 58536.90740$$

$$N(t) = 58536.90740 - \frac{58536.90740}{e^{-1.575029016 \cdot 10^{-8} t^4 + 0.00002500972663 t^3 - 0.005188789106 t^2 + 0.4408998095 t - 13.84173837} + 1}$$

$$Chi2 := 1582.299972$$

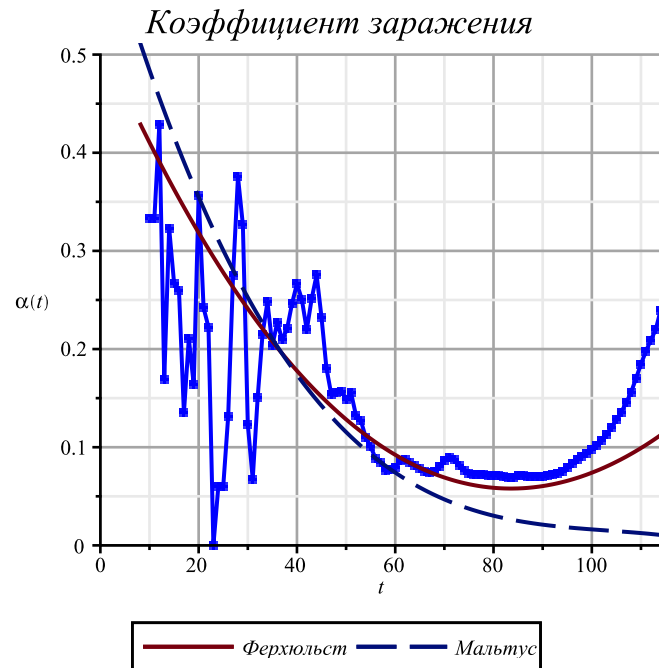
Next day forecast: 54964

The level of 0.5 M is reached at 50 apr
 The level of 0.85 M is reached at 76 apr

Approximation of the infection schedule by solving the Malthus equation

$$N(t) = e^{-1.340055772 \cdot 10^{-7} t^4 + 0.00005162975904 t^3 - 0.007638568025 t^2 + 0.5285831666 t - 3.882074732}$$

$$[0.517240896200000, -0.0114372479000000, 0.0000763522042600000, -6.300116064 \cdot 10^{-8}]$$



```
> df:=unapply(diff(f(i),i),i): ddf:=unapply(diff(f(i),i,i),i):
```

```
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(90,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(90,dd+nops(T))),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..80,1..M*1.1],labels=[t,N(t)],gridlines=true
```



```

);

display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(120,dd+nops(T))),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

```

```

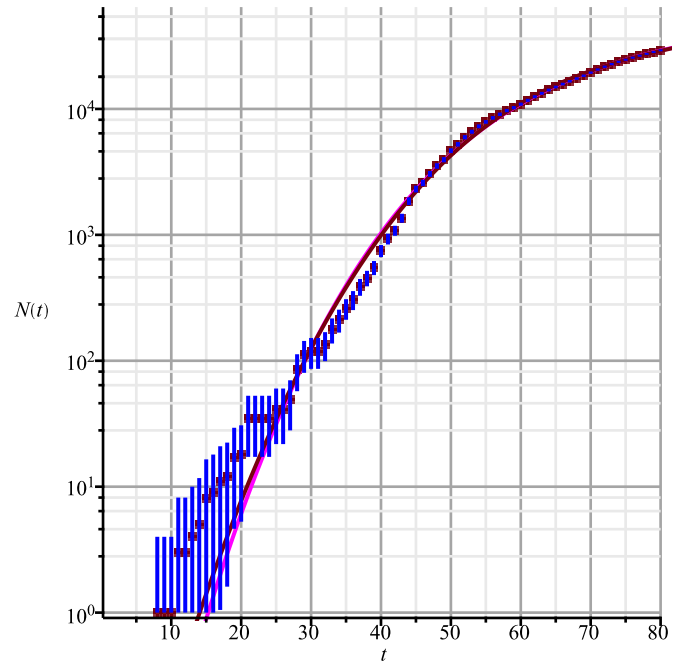
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),90)),
  plot(10*df(i-dd),i=1+dd..max(dd+nops(T),120),color=black),
  plot(100*ddf(i-dd),i=1+dd..max(dd+nops(T),120),color=gray),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..80,-M*0.3..M*1.1],labels=[t,N(t)],gridlines=true
);

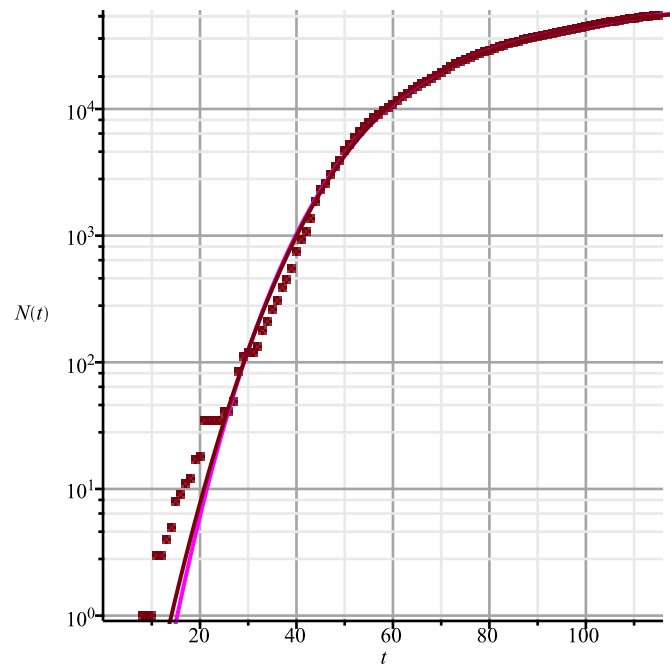
```

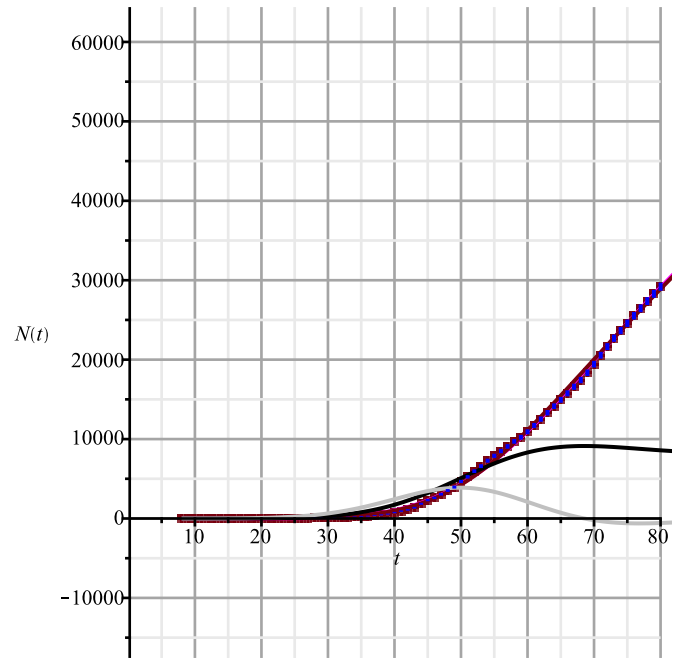
```

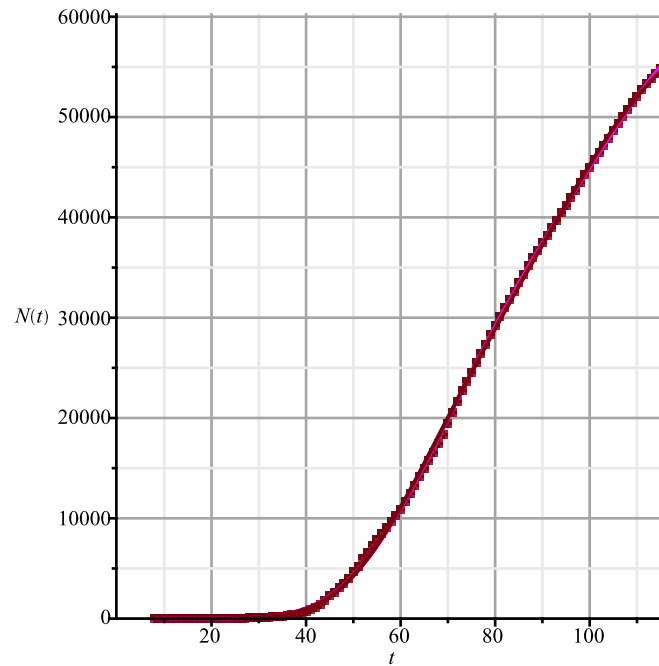
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),120)),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

```



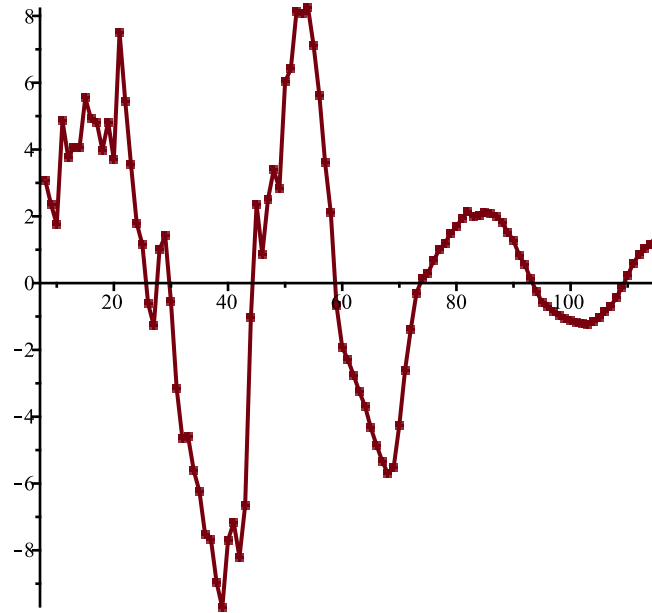






```
> dT:=[i, (T[i-dd]-f(i-dd))/sigma(f(i-dd))] $ i=1+dd..dd+nops(T):
display( plot(%), plot(% ,style=point,symbolsize=8,symbol=solidcircle),title = ` ` ,titlefont=
[roman,20] );
```

Девияция



```
> ===== ` ;  
`FORECAST` ;  
===== ` ;  
  
=====   
FORECAST   
=====   
  
> proc3:=proc (E)  
  E[1]*convert (map (X->X^coeff (E[2] ,X,1) ,M) , `*` ) ;  
end:  
  
proc2:=proc (X,E)  
  proc3 (E) * (coeff (E[3] ,X,1) -coeff (E[2] ,X,1)) ;  
end:  
  
proc1:=proc (X)  
  convert (map (E->proc2 (X,E) ,L) , `+` ) ;  
end:
```

```
> A:='A': B:='B': C:='C': Q:='Q': M:=[A,B,C,Q];
```

```
L:=  
  [(A+C)*P[`01`],0,A],  
  [(B/K)*P[`12`],A,B],  
  [P[`23`],B,C],  
  [P[`10`],A,0], [P[`20`],B,Q], [P[`30`],C,0]  
]: Matrix(%);
```

```
eqs:=map(X->Diff(X,t)=procl(X),M); Vector(%);
```

$M := [A, B, C, Q]$

$$\begin{bmatrix} (A+C)P_{01} & 0 & A \\ \frac{BP_{12}}{K} & A & B \\ P_{23} & B & C \\ P_{10} & A & 0 \\ P_{20} & B & Q \\ P_{30} & C & 0 \end{bmatrix}$$

$$eqs := \left[\frac{\partial}{\partial t} A = (A+C)P_{01} - \frac{BP_{12}A}{K} - P_{10}A, \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B, \frac{\partial}{\partial t} C = P_{23}B - P_{30}C, \frac{\partial}{\partial t} Q = P_{20}B \right]$$

$$\left[\begin{array}{l} \frac{\partial}{\partial t} A = (A + C) P_{01} - \frac{B P_{12} A}{K} - P_{10} A \\ \frac{\partial}{\partial t} B = \frac{B P_{12} A}{K} - P_{23} B - P_{20} B \\ \frac{\partial}{\partial t} C = P_{23} B - P_{30} C \\ \frac{\partial}{\partial t} Q = P_{20} B \end{array} \right]$$

(6)

```
> v:=M; alpha:='alpha': K:=k0; tA:=[-7,15,35,50,58,62,97,nops(T)+dd]; kA:=['k1x||i' $ i=1..nops(tA)
];
par:=[d0,k0,op(kA),k2a,k2b,k2c,k3]; kappa:=0; 0.011/365;
param:=[
  P[`01`] = kappa, P[`12`] = alpha(t,op(kA)), P[`23`] = beta(t,k2a,k2b,k2c),
  P[`10`] = kappa, P[`20`] = k3, P[`30`] = kappa
];
init:=[ A(-d0)=K, B(-d0)=1, C(-d0)=0, Q(-d0)=0 ];
```

$$v := [A, B, C, Q]$$

$$K := k0$$

$$tA := [-7, 15, 35, 50, 58, 62, 97, 115]$$

$$kA := [k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8]$$

$$par := [d0, k0, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8, k2a, k2b, k2c, k3]$$

$$\kappa := 0$$

$$0.00003013698630$$

$$param := [P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b, k2c), P_{10} = 0, P_{20} = k3, P_{30} = 0]$$

$$init := [A(-d0) = k0, B(-d0) = 1, C(-d0) = 0, Q(-d0) = 0]$$

(7)


```
> Eqs:=subs (map (q->q(t), v), Diff=diff, param, eqs); #dsolve(%);
```

$$Eqs := \left[\frac{d}{dt} A(t) = - \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0}, \frac{d}{dt} B(t) \right. \\ \left. = \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0} - \beta(t, k2a, k2b, k2c) B(t) - k3 B(t), \frac{d}{dt} C(t) = \beta(t, k2a, k2b, \right. \\ \left. k2c) B(t), \frac{d}{dt} Q(t) = k3 B(t) \right]$$

```
> N:='N': A:='A': B:='B': C:='C': Q:='Q': val:=valp:
```

```
#alpha:=unapply(simplify(evalf(piecewise(t<tA[1], kA[1], t<tA[2], Lag(t, tA[1..3], kA[1..3]),
# seq(op([t<tA[i+1], (Lag(t, tA[i-1..i+1], kA[i-1..i+1])+Lag(t, tA[i..i+2], kA[i..i+2]))/2]), i=2..nops
(kA)-2),
#t<tA[nops(tA)], Lag(t, tA[nops(tA)-2..nops(tA)], kA[nops(kA)-2..nops(kA)]),
#kA[nops(kA)])), t, op(kA)):
```

```
alpha:=unapply(simplify(evalf(piecewise(t<tA[1], kA[1], t<tA[3], Lag(t, tA[1..4], kA[1..4]),
seq(op([t<tA[i+1], Lag(t, tA[i-1..i+2], kA[i-1..i+2]])], i=3..nops(kA)-2),
t<tA[nops(tA)], Lag(t, tA[nops(tA)-2..nops(tA)], kA[nops(kA)-2..nops(kA)]),
kA[nops(kA)])), t, op(kA)):
```

```
beta:=(t, k2a, k2b, k2c)->piecewise(t<18, 0.001, t<40, k2a, t<100, Lag(t, [40, 80, 100], [k2a, k2b, k2c]), k2c):
beta:=unapply(simplify(evalf(beta(t, k2a, k2b, k2c))), t, k2a, k2b, k2c):
```

```
EQS:=[op(Eqs), op(init)]:
```

```
res:=dsolve(EQS, numeric, map(q->q(t), v), output=listprocedure, parameters=par); assign('v[i]=subs
(res, v[i](t))' $ i=1..nops(v)):
```

```
chi2a:='chi2a': chi2:=unapply(chi2a(x0, xx, kA, x2a, x2b, x2c, x3), x0, xx, op(kA), x2a, x2b, x2c, x3):
```

```
chi2a:=proc(x0, xx, x1, x2a, x2b, x2c, x3) local i; global K; K:=xx;
res(parameters=[corr(par, [x0, xx, op(x1), x2a, x2b, x2c, x3])]):
sum((T[i]-K-A(i+dd))^2/(K-A(i+dd)), i=1..nops(T))+
sum((T2[i]-B(i+dd))^2/B(i+dd), i=1..nops(T2))+
sum((T3[i]-Q(i+dd))^2/Q(i+dd), i=1..nops(T2))+
sum((T1[i]-C(i+dd))^2/C(i+dd), i=1..nops(T1));
end:
```

```

chi2(op(pr(val))); val:=findMin(chi2,val); chi2(op(%));

#plot(map(q->q(t),v), t=0..3.0e4, legend=[``,``,``],
#linestyle=[solid,dash,dashdot],gridlines=true);

writedata(cat(Region,`3c.txt`),val);

display(
plot(map(q->q(t),v[1..3]), t=0..300, legend=[``,``,``],
linestyle=[solid,dash,dashdot],gridlines=true),
plot([[seq([i+dd,K_-T[i]],i=1..nops(T))]],style=point,symbolsize=7,symbol=asterisk),
plot([[seq([i+dd,T1[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),
plot([[seq([i+dd,T2[i]],i=1..nops(T2))]],style=point,symbolsize=7,symbol=diamond,color=black),
size=[1000,400],legendstyle=[font=[roman,15]]
): fdisplay(cat(Region,`3c`),%);

```

$$\beta := (t, k2a, k2b, k2c) \mapsto \begin{cases} 0.001 \\ k2a \\ (-0.07500000002 \cdot t + 0.0004166666668 \cdot t^2 + 3.333333334) \cdot k2a + (-5. + 0.1750000000 \cdot t - 0.001250000000 \cdot t^2) \cdot k2 \\ k2c \end{cases}$$

```

res := [t=proc(t) ... end proc, A(t)=proc(t) ... end proc, B(t)=proc(t) ... end proc, C(t)=proc(t) ... end proc, Q(t)=proc(t)

```

```

...

```

```

end proc]

```

```

[13.44258404, 62802.67494, 0.1012133281, 0.1111242458, 0.2115507857, 0.1595470238, 0.08751331813, 0.08130220975, 0.07749483653,
0.1277152111, 0.007412379613, 0.01037824493, 0.0236434147, 0.0006037801923]

```

```

6540.24922696382

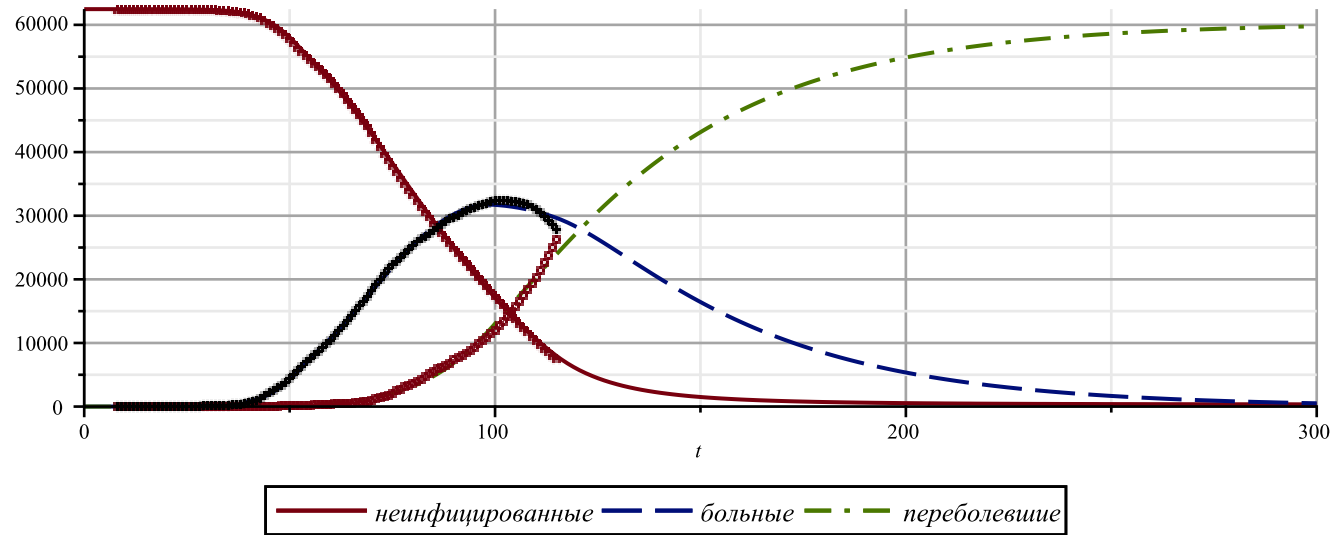
```

6540.24922696382
6514.39646472438
6504.73977536819
6500.63997791507
6497.13965922340
6494.79548185626
6491.99939655040
6490.34764042584
6487.42438261371
6485.48963220800
6472.90171250359
6463.09681253949
6438.95535228891
6433.18423900971
6428.39102323441
6425.75685755777
6423.59982216689
6422.00606602268
6420.12754268654
6418.82953784647
6417.28381385297
6415.78191814709
6410.56729555532
6405.39522910533
6404.51018455419
6403.37727533264
6402.86905877495

val := [13.4846484991988, 62475.3056039865, 0.101588243810236, 0.111681085884875, 0.212273943769069, 0.157013723139909,
0.0865036190301633, 0.0812114241836506, 0.0771971808293624, 0.128032564036750, 0.00736171705530521, 0.0103840854353630,
0.0235902660839014, 0.000602486682783757]

6402.86905877495

Mosobl3c.jpg



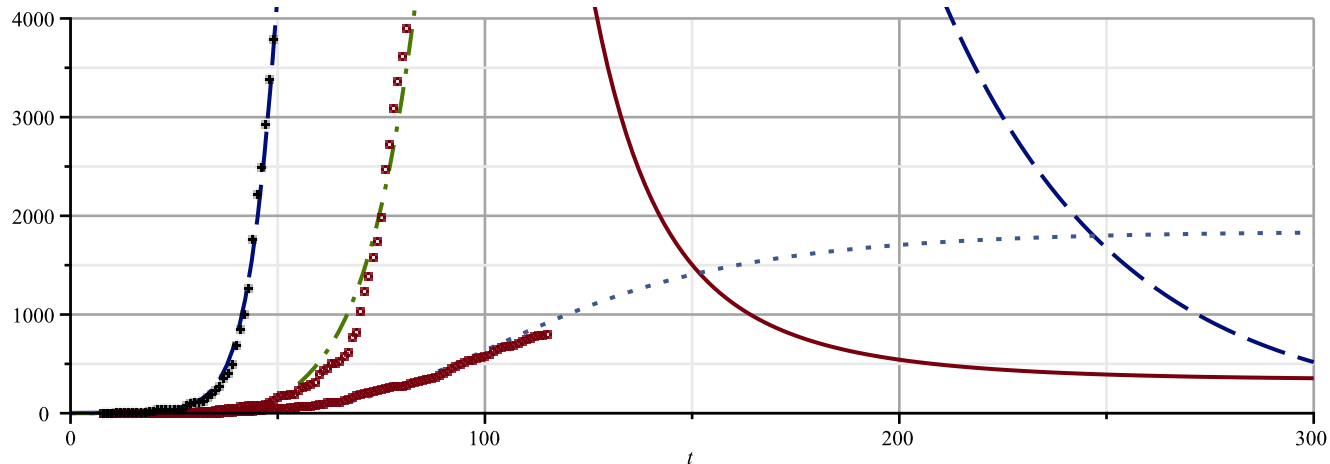
```
> val;
```

```
[13.4846484991988, 62475.3056039865, 0.101588243810236, 0.111681085884875, 0.212273943769069, 0.157013723139909,  
0.0865036190301633, 0.0812114241836506, 0.0771971808293624, 0.128032564036750, 0.00736171705530521, 0.0103840854353630,  
0.0235902660839014, 0.000602486682783757]
```

```
> display(
```

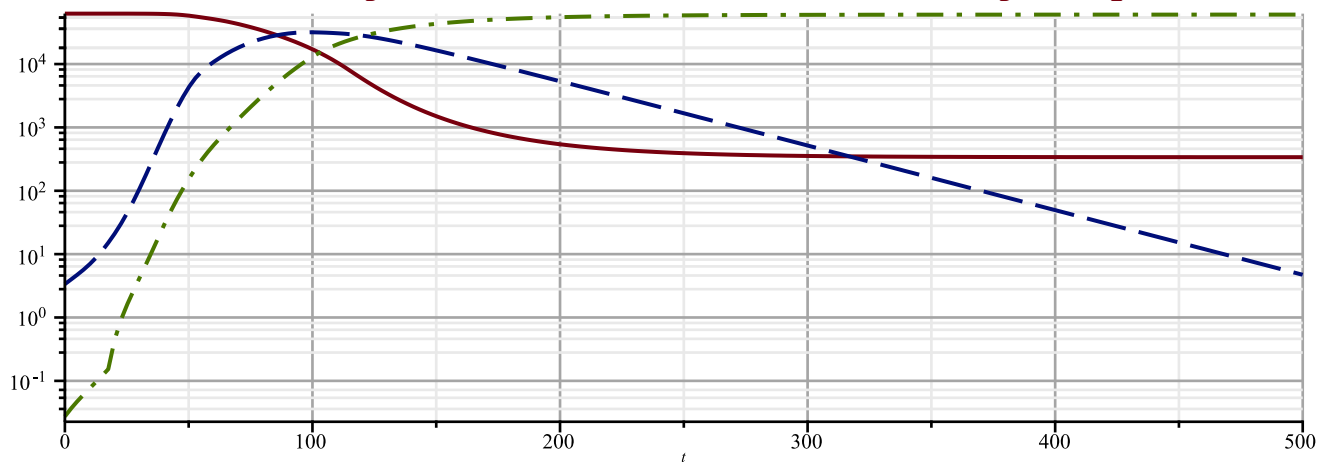
```
plot(map(q->q(t),v), t = 0 .. 300, legend = [ '\ ', '\ ', '\ ', '\ ' ],  
linestyle=[solid,dash,dashdot,dot],gridlines=true),  
plot([[seq([i+dd,K_-T[i]],i=1..nops(T))]],style=point,symbolsize=7,symbol=asterisk),  
plot([[seq([i+dd,T1[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),  
plot([[seq([i+dd,T3[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),  
plot([[seq([i+dd,T2[i]],i=1..nops(T2))]],style=point,symbolsize=7,symbol=diamond,color=black),  
size=[1000,400],legendstyle=[font=[roman,15]],view=[0..300,0..4000]  
);
```

(9)



— неинфицированные — больные -.- переболевшие ··· умершие

```
> logplot(map(q->q(t),v[1..3]),t=0..500,legend=[``,``,``,``],
linestyle=[solid,dash,dashdot],gridlines=true,size=[1000,400],legendstyle=[font=[roman,15]]);
```



— неинфицированные — больные -.- переболевшие

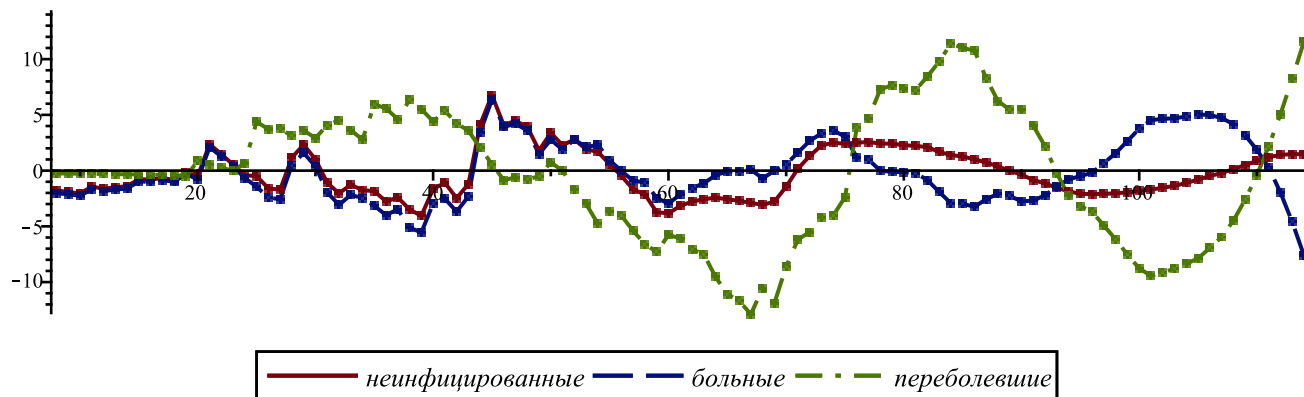
```
> display(
plot([
[[i,(T[i-dd]-(K-A(i)))/sigma(K-A(i))] $ i=1+dd..dd+nops(T)],
[[i,(T2[i-dd]-(B(i)))/sigma(B(i))] $ i=1+dd..dd+nops(T)],
```

```

[[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T) ]
],linestyle=[solid,dash,dashdot],legend=[``,``,``,``]
),
plot([
[[i, (T[i-dd]-(K -A(i)))/sigma(K -A(i))] $ i=1+dd..dd+nops(T) ],
[[i, (T2[i-dd]-(B(i)))/sigma(B(i))] $ i=1+dd..dd+nops(T) ],
[[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T) ]
],style=point,symbolsize=8,symbol=solidcircle),
size=[1000,300],legendstyle=[font=[roman,15]]
): fdisplay(cat(Region,`3c-dev`),%);

```

Mosobl3c-dev.jpg



```

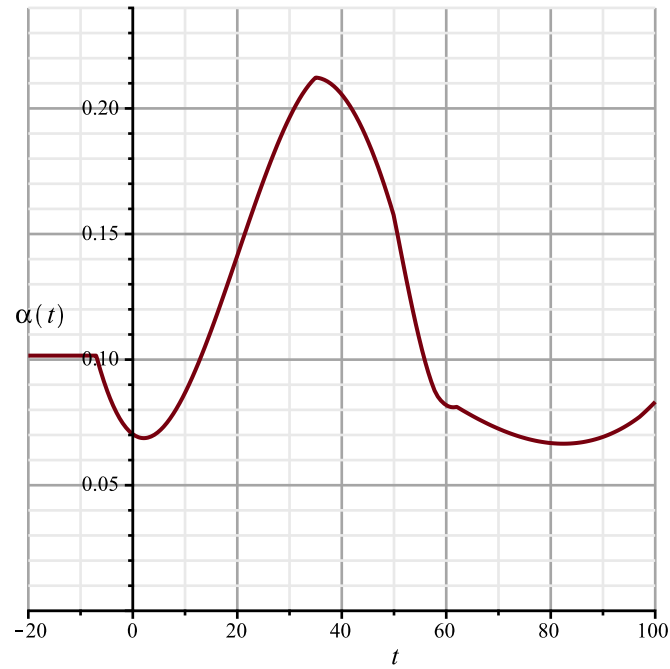
> [seq([i, (
(T[i-dd]-T[i-dd-1]) / (T2[i-dd]+T2[i-dd-1]) / ((1-T[i-dd]/K_) + (1-T[i-dd-1]/K_))
)*4, i=1+dd+1..nops(T)+dd)]: [seq([%[i][1], (%[i-1][2]+ %[i][2]+ %[i+1][2])/3], i=2..nops(%)-1)]:
Palpha:=display(plot([%], color=blue), plot([%], style=point, symbolsize=8, symbol=solidcircle, color=
blue)):
#display(% , gridlines=true, labels=['t', 'alpha(t)'], labelfont=[roman,15], view=[0..nops(T)+dd, 0.
.0.9]);

subs(corr(par, val), alpha(t, op(kA)));
plot(% , t=-20..100, gridlines=true, labels=['t', 'alpha(t)'], labelfont=[roman,15], view=[-20..100, 0.
.0.24]):
fdisplay(cat(Region,`3c-zar`), %); display([Palpha, %], title = ``, titlefont=
[roman,20]);

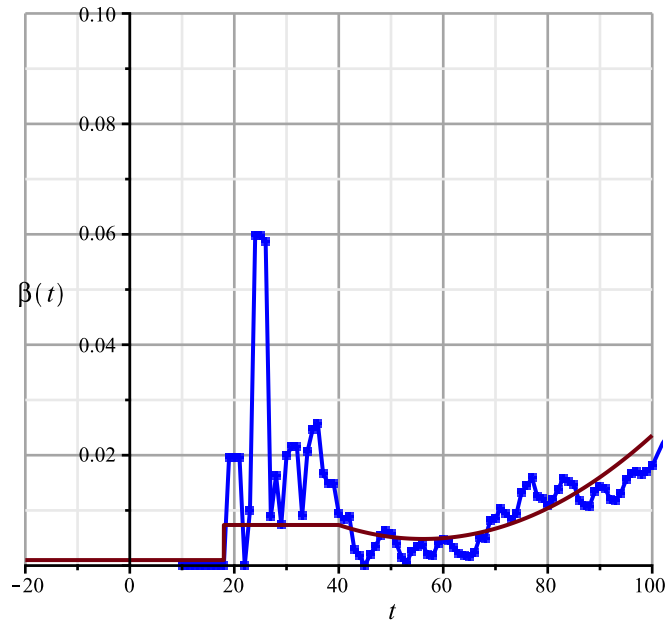
```

	0.101588243810236	$t < -7.$
}	$-6.27705366039718 \cdot 10^{-6} t^3 + 0.000378743720065812 t^2 - 0.00151036214322235 t + 0.0703042371057076$	$t < 35.$
	$6.03002590494697 \cdot 10^{-7} t^3 - 0.000309261902713840 t^2 + 0.0193018079504592 t - 0.110297238946187$	$t < 50.$
	$0.0000313799528517988 t^3 - 0.00471036580242839 t^2 + 0.224891836166461 t - 3.23415769372680$	$t < 58.$
	$-0.0000126221851821180 t^3 + 0.00276999767210657 t^2 - 0.197352681073602 t + 4.67742672945581$	$t < 62.$
	$4.29247182985156 \cdot 10^{-7} t^3 - 0.0000621631511551986 t^2 + 0.00149894275450570 t + 0.124930499642958$	$t < 97.$
	$0.0000554505779072480 t^2 - 0.00893133454643109 t + 0.421802145194817$	$t < 115.$
	0.128032564036750	$115. \leq t$

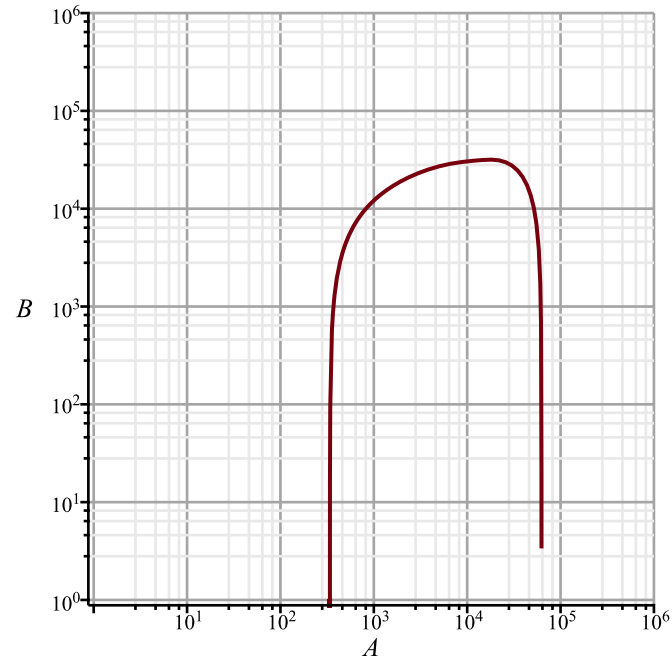
Mosobl3c-zar.jpg



Коэффициент выздоровления



```
> plot([v[1](t),v[2](t),t=0..3.0e4],labels=[v[1],v[2]],labelfont=[roman,15],gridlines=true,axis[1]=[mode=log],axis[2]=[mode=log],view=[10^0..10^6,10^0..10^6]);
```



```

> res:=solve(map(rhs,eqs[1..2]),v[1..2]); res:=res[2]; evalf(subs(param,t=100,res));

J:=Matrix(subs(res,map(q->grad(rhs(q),v[1..2]),eqs[1..2]))); J:=evalf(subs(param,corr(par,val),t=
100,J));
evalm(%-lambda): collect(Determinant(%),lambda);

#evalf(subs(param,corr(par,val),t=100,%));
solve(%,{lambda});

```

$$\text{res} := \left[\left[A = \frac{C P_{01}}{P_{10} - P_{01}}, B = 0 \right], \left[A = \frac{k0 (P_{23} + P_{20})}{P_{12}}, B = \frac{C P_{01} P_{12} + k0 P_{01} P_{20} + k0 P_{01} P_{23} - k0 P_{10} P_{20} - k0 P_{10} P_{23}}{P_{12} (P_{23} + P_{20})} \right] \right]$$

$$\text{res} := \left[A = \frac{k0 (P_{23} + P_{20})}{P_{12}}, B = \frac{C P_{01} P_{12} + k0 P_{01} P_{20} + k0 P_{01} P_{23} - k0 P_{10} P_{20} - k0 P_{10} P_{23}}{P_{12} (P_{23} + P_{20})} \right]$$

$$\left[A = \frac{k0 (k2c + k3)}{-0.024258761 k1x6 + 0.90476191 k1x7 + 0.119496860 k1x8}, B = 0. \right]$$

$$J := \begin{bmatrix} P_{01} - \frac{C P_{01} P_{12} + k_0 P_{01} P_{20} + k_0 P_{01} P_{23} - k_0 P_{10} P_{20} - k_0 P_{10} P_{23}}{(P_{23} + P_{20}) k_0} & -P_{10} & -P_{23} & -P_{20} \\ \frac{C P_{01} P_{12} + k_0 P_{01} P_{20} + k_0 P_{01} P_{23} - k_0 P_{10} P_{20} - k_0 P_{10} P_{23}}{(P_{23} + P_{20}) k_0} & & & 0 \end{bmatrix}$$

$$J := \begin{bmatrix} 0. & -0.0241927527666851 \\ 0. & 0. \end{bmatrix}$$

$$\lambda^2$$

$$\{\lambda=0\}, \{\lambda=0\}$$

(10)

```
> N:='N': A:='A': B:='B': C:='C': Q:='Q':
```

```
param:=[
  P[`01`] = kappa, P[`12`] = k1, P[`23`] = k2,
  P[`10`] = kappa, P[`20`] = k3, P[`30`] = k4
];
corr(par, val);
subs(param, eqs); R:=solve(%, [k1, k2, k3, k4])[1];
```

```
X:='X': X1:='X1': subs(R, Diff(A, t) = -X1[1][i][2], Diff(B, t) = X1[2][i][2], Diff(C, t) = X1[3][i][2], Diff
(Q, t) = X1[4][i][2], A = k0 - X[1][i][2], B = X[2][i][2], C = X[3][i][2], Q = X[4][i][2], [k1, k2, k3, k4]): XX:=
unapply(subs(k0=K_, %), i):
```

$$param := [P_{01} = 0, P_{12} = k1, P_{23} = k2, P_{10} = 0, P_{20} = k3, P_{30} = k4]$$

```
d0 = 13.4846484991988, k0 = 62475.3056039865, k1x1 = 0.101588243810236, k1x2 = 0.111681085884875, k1x3 = 0.212273943769069, k1x4
= 0.157013723139909, k1x5 = 0.0865036190301633, k1x6 = 0.0812114241836506, k1x7 = 0.0771971808293624, k1x8
= 0.128032564036750, k2a = 0.00736171705530521, k2b = 0.0103840854353630, k2c = 0.0235902660839014, k3
= 0.000602486682783757
```

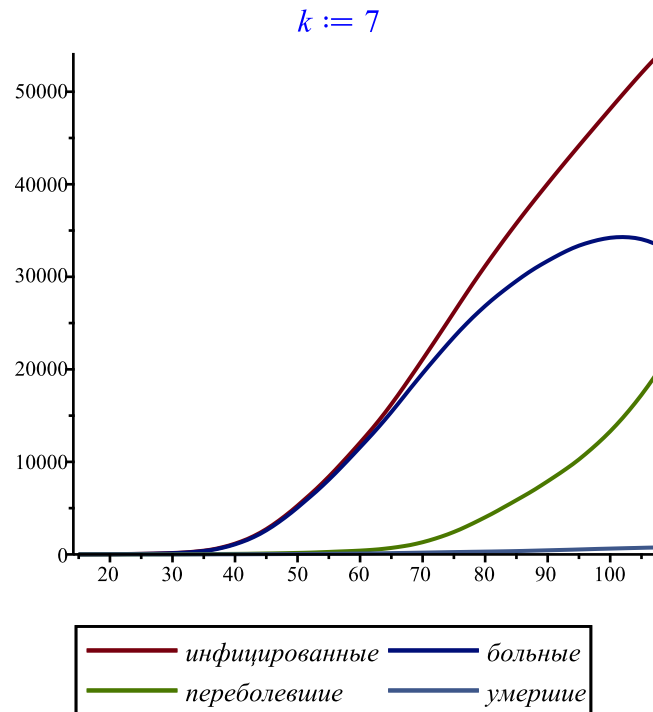
$$\left[\frac{\partial}{\partial t} A = -\frac{B k_1 A}{k_0}, \frac{\partial}{\partial t} B = \frac{B k_1 A}{k_0} - k_2 B - k_3 B, \frac{\partial}{\partial t} C = k_2 B - C k_4, \frac{\partial}{\partial t} Q = k_3 B \right]$$

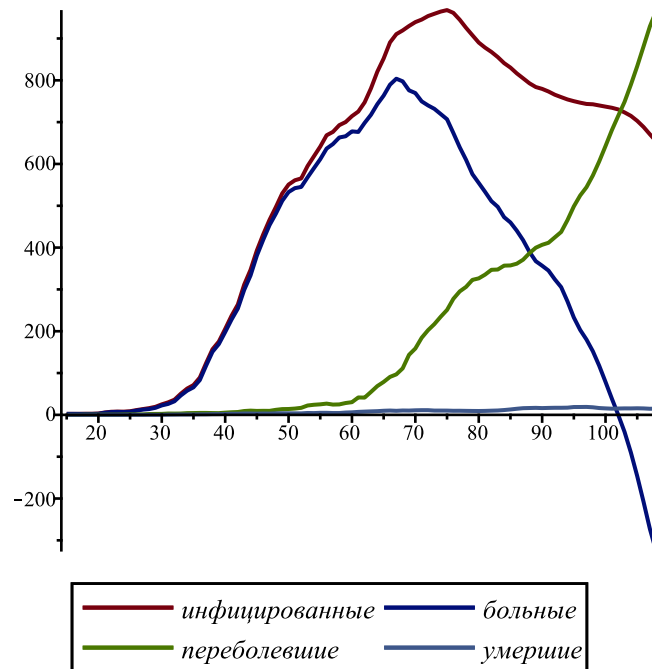
$$R := \left[k1 = -\frac{\frac{\partial}{\partial t} A k0}{A B}, k2 = -\frac{\frac{\partial}{\partial t} A + \frac{\partial}{\partial t} B + \frac{\partial}{\partial t} Q}{B}, k3 = \frac{\frac{\partial}{\partial t} Q}{B}, k4 = -\frac{\frac{\partial}{\partial t} A + \frac{\partial}{\partial t} B + \frac{\partial}{\partial t} Q + \frac{\partial}{\partial t} C}{C} \right] \quad (11)$$

```

> k:=7;
X:=map(q->[seq([i+dd, (ssum(q[i+j], j=-k..k)) / (2*k)], i=1+k..nops(q)-k)], [T, T2, T1, T3]):
plot(%, legend=[' ', ' ', ' ', ' '], legendstyle=[font=[roman, 15]]);
X1:=map(q->[seq([i+dd, (q[i+k]-q[i-k]) / (2*k)], i=1+k..nops(q)-k)], [T, T2, T1, T3]):
plot(%, legend=[' ', ' ', ' ', ' '], legendstyle=[font=[roman, 15]]);

```





> k:=0;

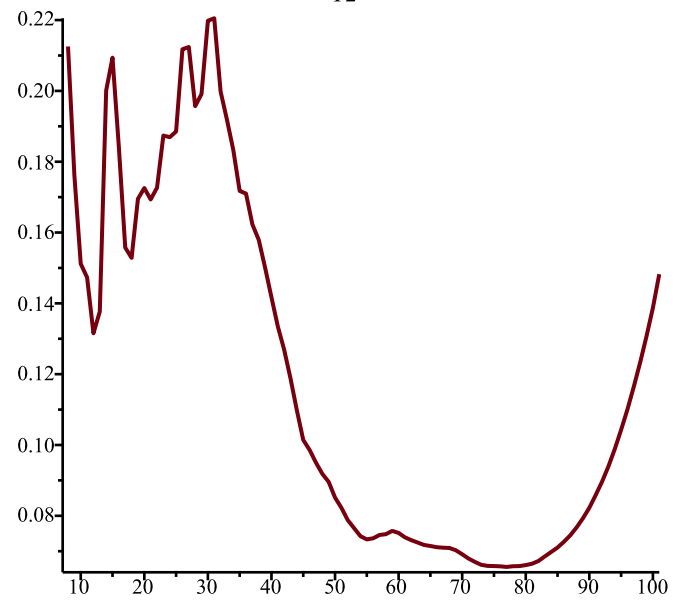
```
[seq([i+dd+k,XX(i)[1]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`12`],titlefont=[roman,20]);
```

```
[seq([i+dd+k,XX(i)[2]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`23`],titlefont=[roman,20]);
```

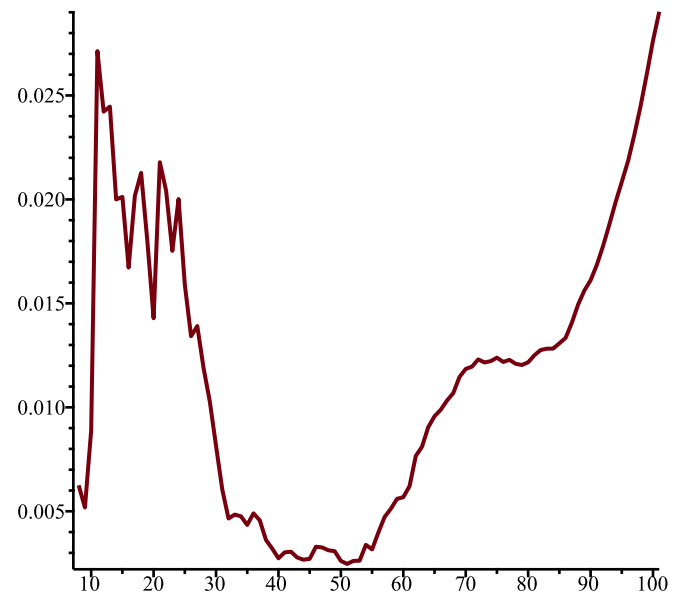
```
[seq([i+dd+k,XX(i)[3]],i=1..nops(X[1]))]: [seq([%[i][1],(ssum(%[i+j][2],j=-k..k))/(2*k+1)],i=1+k..nops(%)-k)]:
plot([%],title=P[`20`],titlefont=[roman,20]);
```

k := 0

P_{12}



P_{23}



P_{20}

